

Decision Tree Based Online Voltage Security Assessment Using PMU Measurements

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Contents

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- Classification based on Decision Trees
- The Proposed Scheme
 - Offline DT Building
 - Periodic DT Updating
 - Online Voltage Security Assessment
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- Conclusions and Future Work

Main Problems

- Deregulation has resulted in market driven environments
- Lack of sufficient coordination among different operating entities
- Increase in load demand has outpaced the growth of generation capacity
- Difficulty of installing new transmission lines due to environmental and investment concerns
- Power networks are operated under greater stress
- Critical contingencies may violate voltage security limits and even initiate voltage instability
- Historically large scale blackouts were caused by multiple events in a short time period

Voltage Stability Problem

- The ability to maintain bus voltage magnitudes within normal operating limits both at normal operating conditions and after disturbances
- Usually caused by the lack of sufficient reactive power support to a load area with a large amount of reactive power demand
- Initiated by a serious disturbance like a fast load increase or a contingency
- Voltage magnitudes progressively decline to an unacceptable level
- Once the voltage magnitude starts to decline, the loads such as motors try to recover the voltage magnitudes by consuming more reactive power
- It can exhaust the available reactive power reserve and further cause the voltage magnitudes to drop

Voltage Stability Problem

- Not only affect the local load area, but can also spread throughout adjacent areas of the power system
- As voltage stability is largely impacted by load components, especially induction motors, voltage stability is also referred to as *load stability*

Challenge of Online Security Assessment



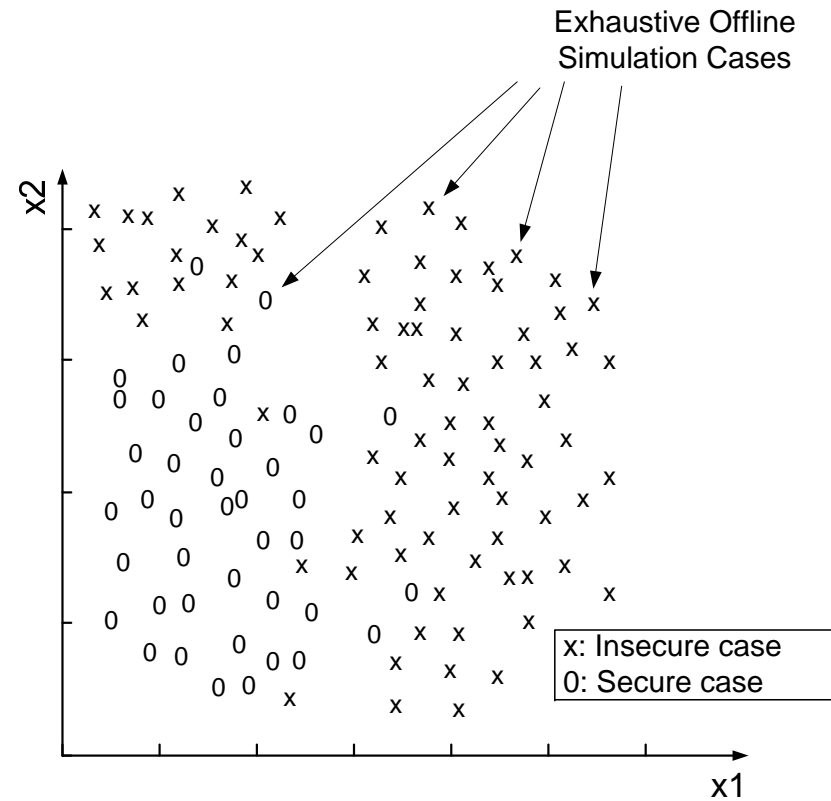
- Large interconnected power systems are highly nonlinear
- With thousands of system states
- Detailed analysis in near real time horizon is a great challenge due to the large computational burden
- Oversimplification of system model will reduce assessment accuracy
- Traditional method performs security analysis on selected contingencies in the interval of several minutes
- Not rapid enough to arm timely control actions for fast events
- Hard to indicate secure operation boundaries

A New Assessment Tool

- Need for a new assessment tool
 - Capture full system behavior accurately
 - Fast enough to arm control actions as soon as a vulnerable situation occurs
 - Effectively characterize the vulnerability of the current operating condition (OC)
- Solution – Decision Trees (DTs)
 - The underlying principle:
 - “Derive an internal rule (in terms of thresholds) between multiple inputs and the predictive objective that can accurately classify both the foreseen and unforeseen cases”

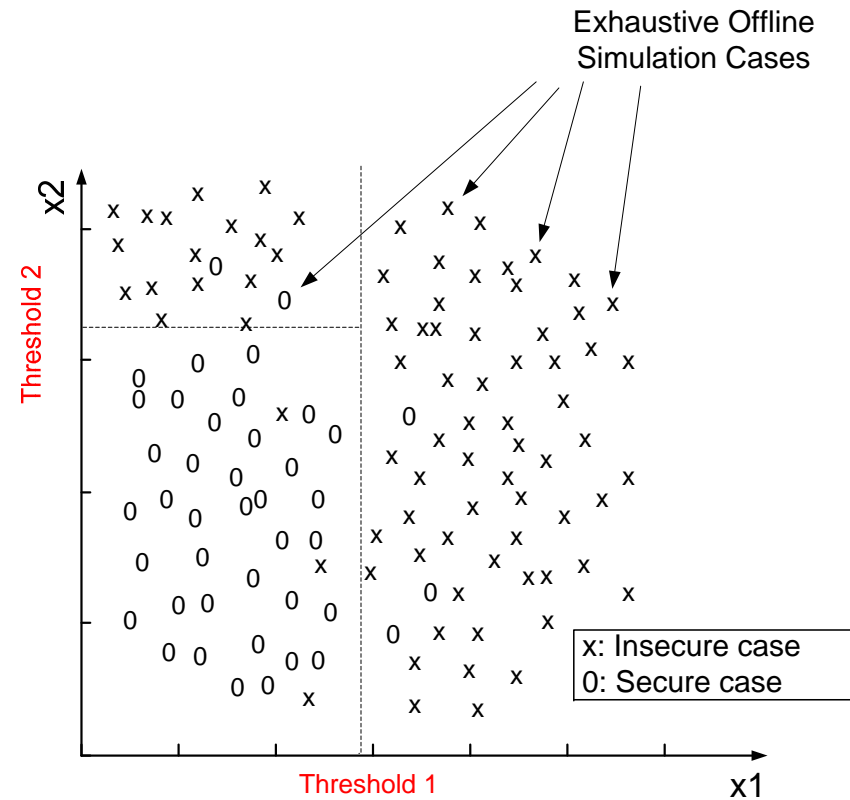
Basic Idea

- Exhaustive offline study
- Select predictors



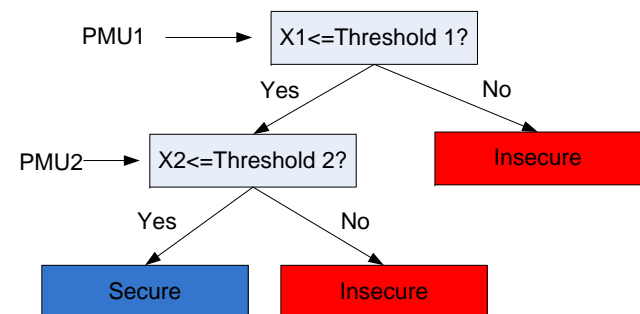
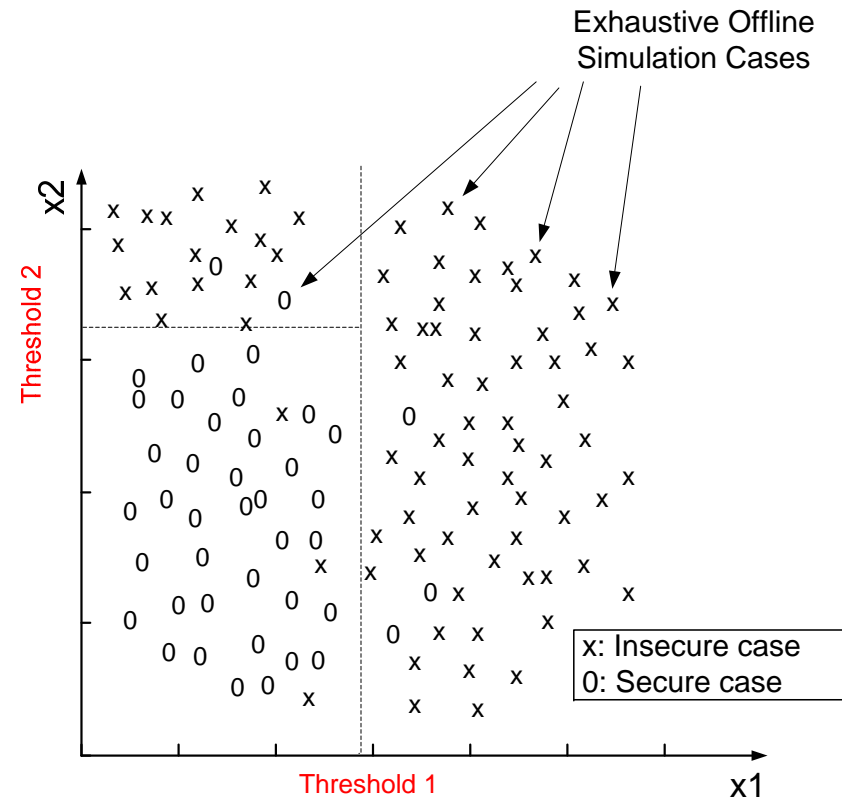
Basic Idea

- Exhaustive offline study
- Select predictors
- Discover underlying rules



Basic Idea

- Exhaustive offline study
- Select predictors
- Discover underlying rules
- Compare PMU measurement with offline determined thresholds
- Obtain a prediction result



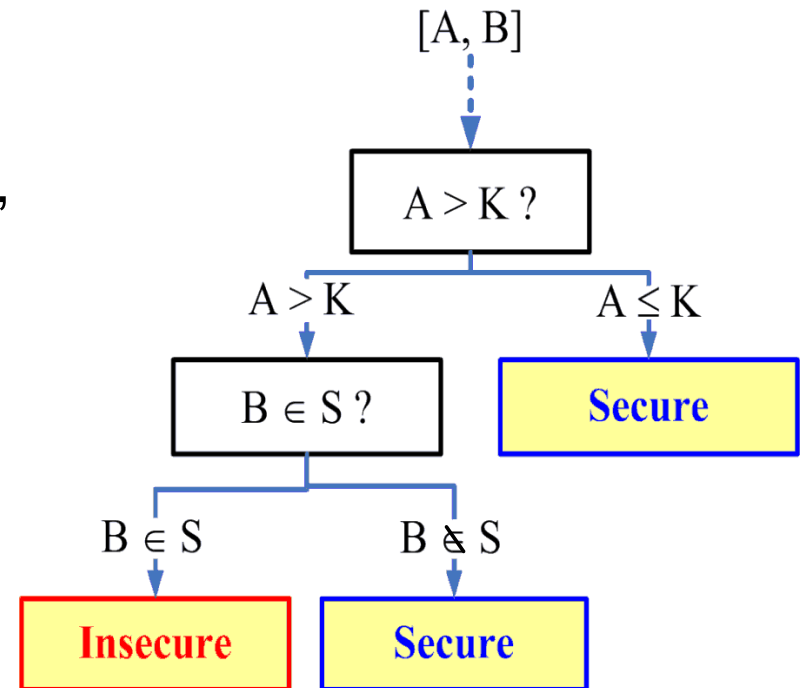
Classification Based on Decision Trees



- Flowchart representing a classification system or predictive model for an object
- Structured as a sequence of simple questions based on critical attributes (CAs)
- Answers to these questions trace a path down the tree
- Terminal node determines the final classification or prediction result
- In 1984, Breiman introduced the CART (Classification and Regression Trees) methodology

Example of Classification Tree

- Object is characterized by a vector of CAs, voltage magnitude violation, thermal violation, transient stability, voltage stability, etc
- For numerical attribute A , question compares it with a threshold (K)
- For categorical attribute B , question checks if it belongs to a particular set (S)
- A class (**Secure** or **Insecure**) is assigned to the object at the terminal node



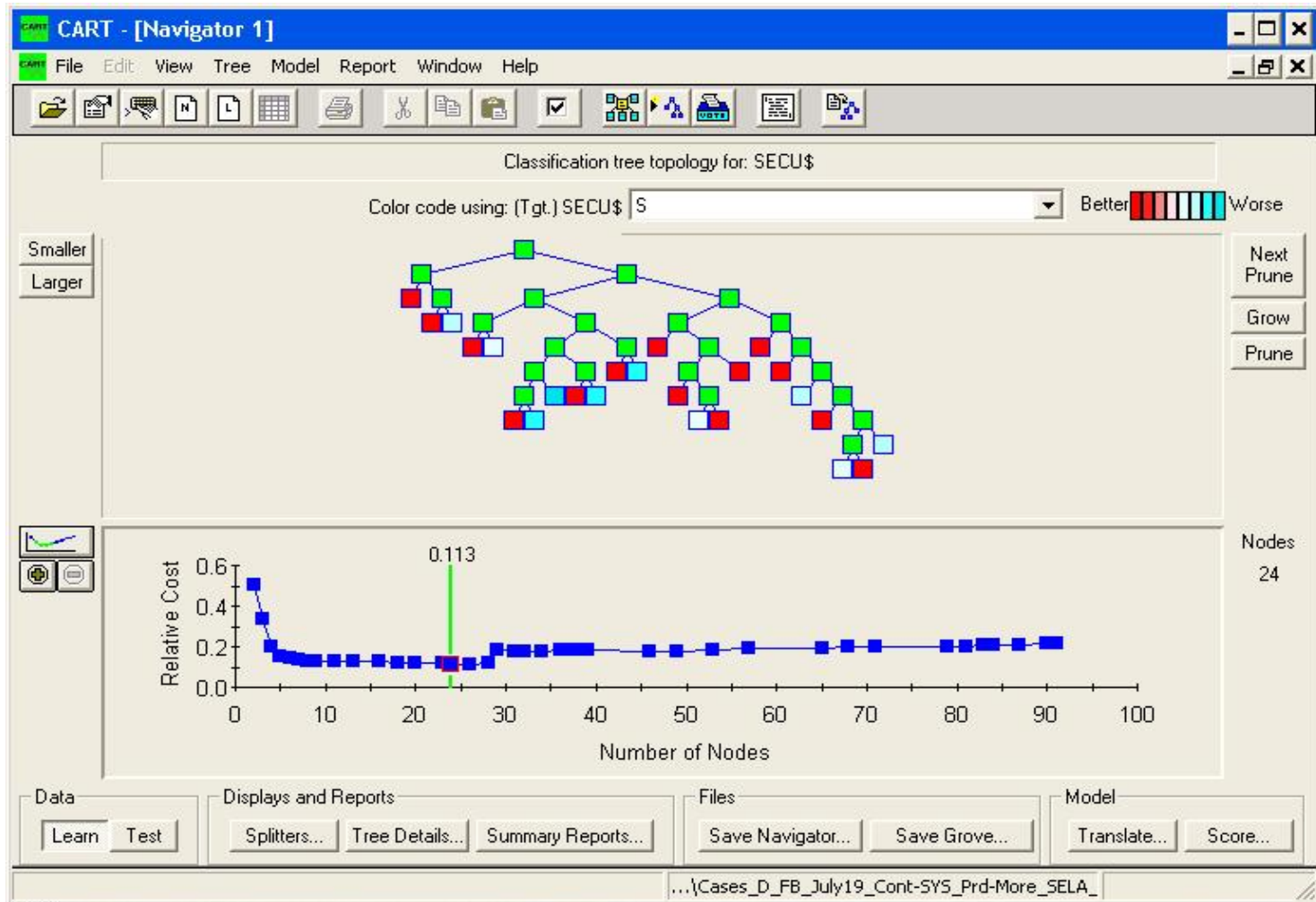
Building a Good DT

- Preparation
 - A sufficiently large database
 - Cases with different classifications are separated **randomly** into a learning set (LS) and a test set (TS)
 - Predictors are selected from available PMU measurements
- DT growing
 - A maximal binary tree is grown by recursively splitting the learning set
 - At each splitting, questions about predictors are scored by purities of two child nodes

Building a Good DT

- Question with highest score is selected and called “Critical Splitting Rule” (CSR)
- **Parameter used in CSR is CA**
- As the tree grows, nodes become more homogeneous
- DT pruning:
 - The maximal tree is pruned step by step to generate a series of DT’s with descending sizes
 - Performance of each DT is checked on the test set
 - Minimizing the misclassification cost
 - Meeting additional requirements (about **size**, **correctness rate**, ...)

DT Training in CART



Performance Parameters

- Main parameters defined by the CART methodology:

- R^{ts} --- Misclassification cost

$$R^{ts} = \frac{1}{N^{ts}} \sum_i c(i | j) \cdot N_{ij}^{ts}$$

- CR_i^{ts} --- Correctness rate for classifying class- i cases

$$CR_i^{ts} = N_{ii}^{ts} / N_i^{ts} \times 100\%$$

- $c(i|j)$ --- Cost of misclassifying a class- j case as class- i

- N^{ts} --- Number of test cases

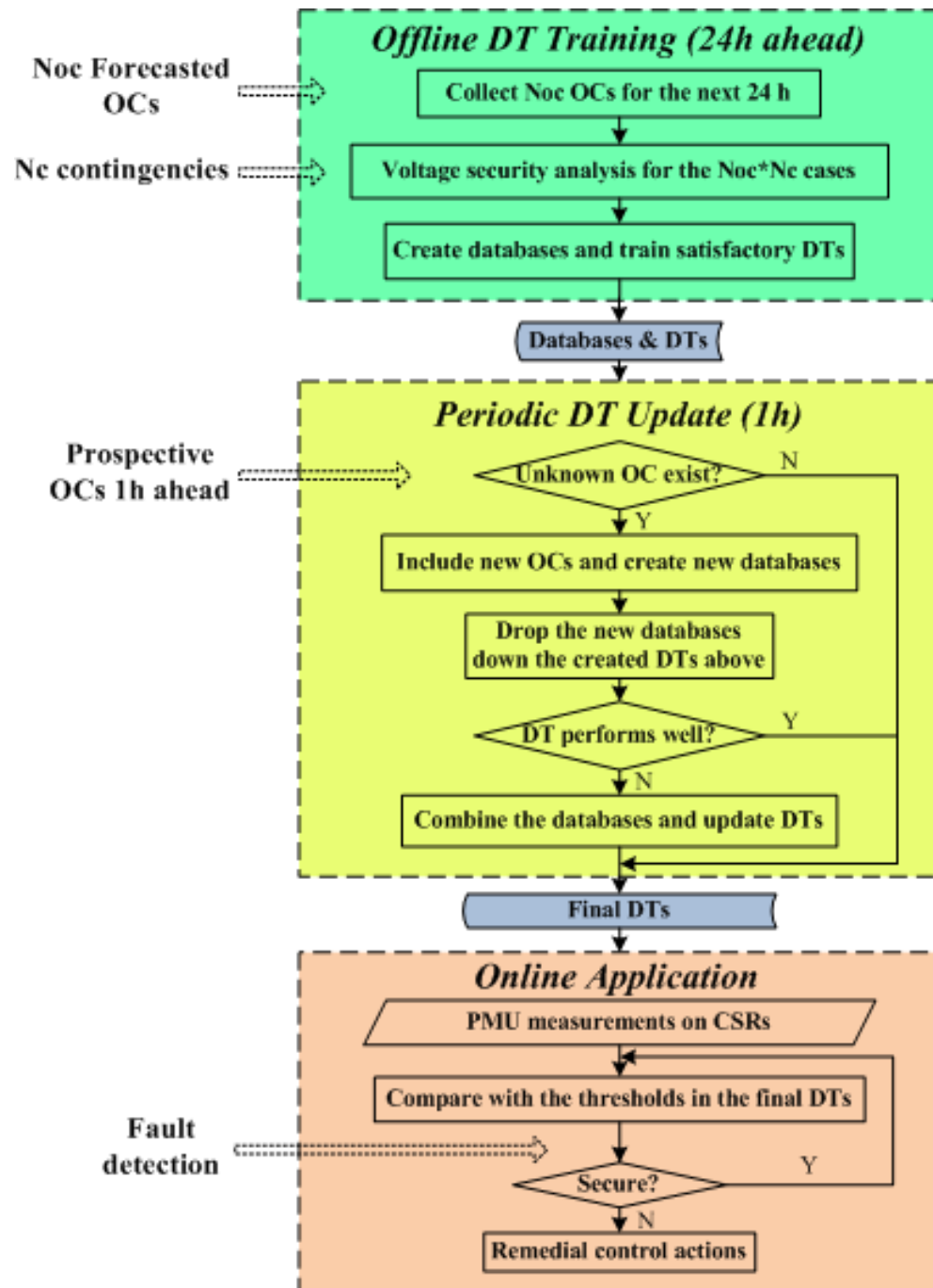
- N_{ij}^{ts} --- Number of the class- j cases predicted as class- i

Critical Attributes (CAs)

- The CAs are measured simultaneously by the PMUs
- The thresholds of the CAs define an operating nomogram
- If the OC drives a CA to violate its threshold then arming could be performed
- If the contingency corresponding to the CA threshold occurs then preventive action will have to be taken to maneuver the system to a safe OC

Proposed Scheme

- Offline DT Training (24 hours ahead)
- Periodic DT update (every hour)
- Online security assessment & control



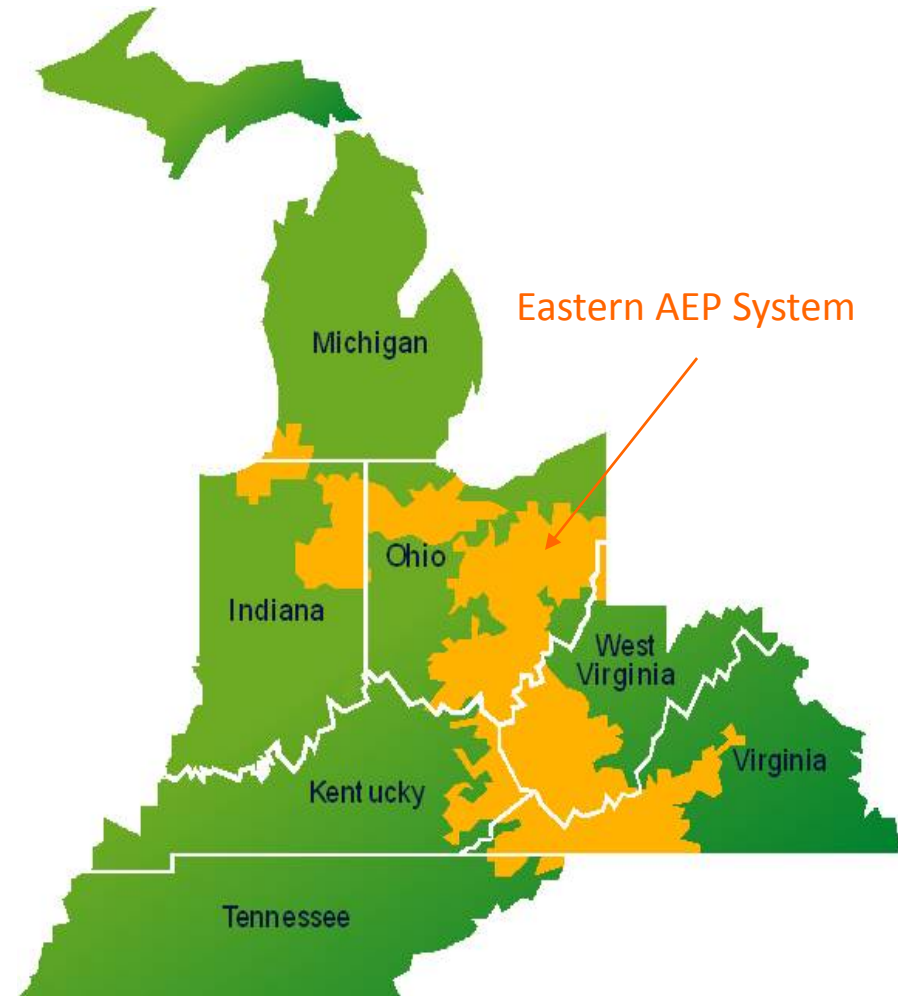
System Analysis Tools

- DSA^{TOOLS}: Dynamic Security Analysis Tool, Powertech, Canada
 - PSAT: Powerflow & Short-circuit Analysis Tool, generation and tuning operating conditions
 - VSAT: Voltage Security Assessment Tool, voltage security analysis
- CART: Classification and Regression Trees, Salford Systems, CA, training and testing decision trees
- MATLAB and VC++: data collection and conversion, database creation, etc



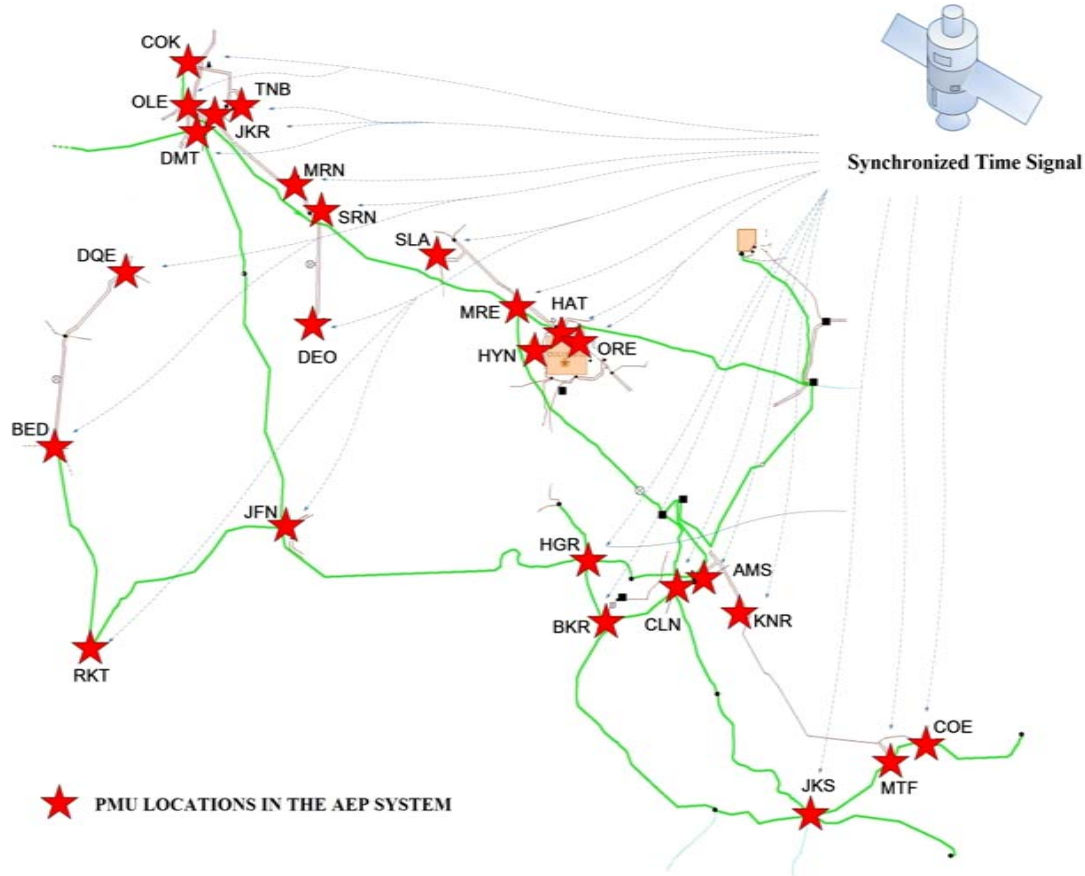
Implementation on the AEP system

- AEP system
 - A subset of the Eastern Interconnection in North America
 - Cover several states, serve about 10% of load demand in Eastern Interconnection
 - Divided into western AEP and eastern AEP
 - Operational model of eastern AEP:
 - 2414 buses, 116 generators, 2416 transmission lines
 - Voltage level: 4 kV to 765 kV
 - 39,000-mile network





PMU Locations in the Eastern AEP System ^{PSERC}

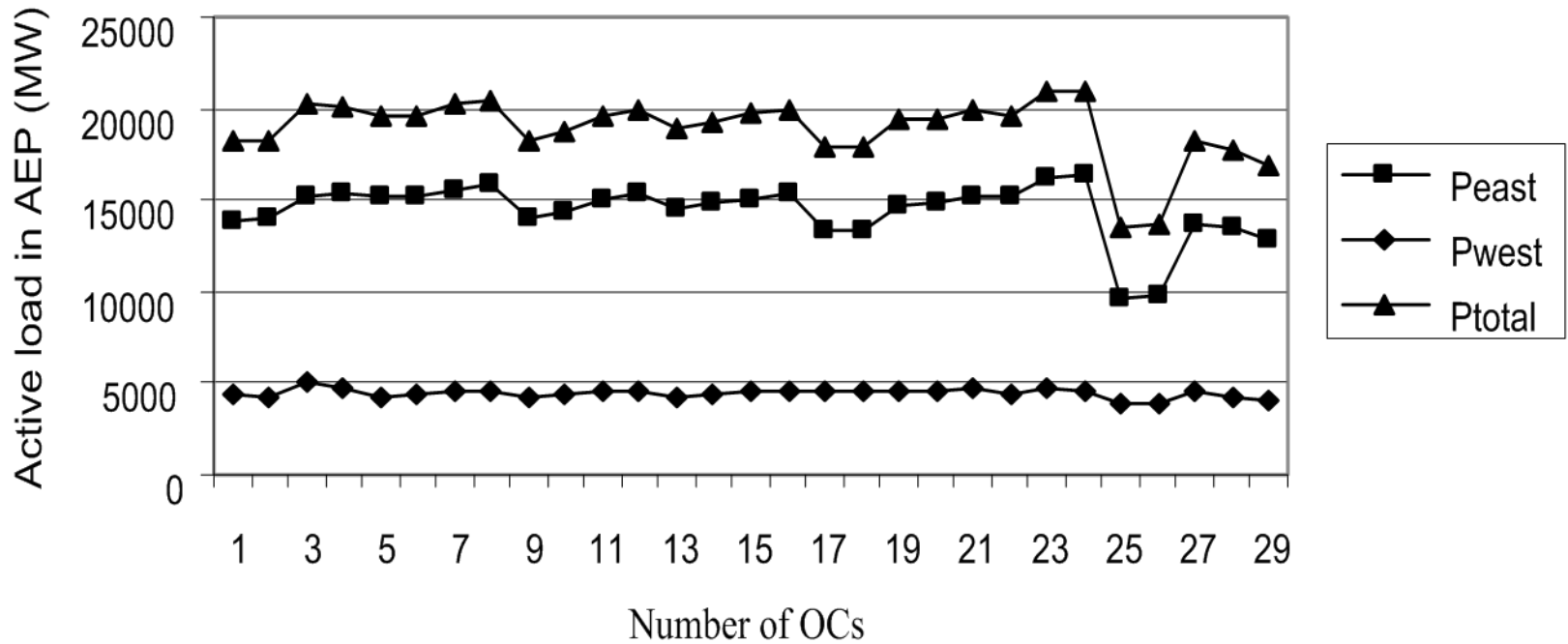


- 27 phasor measurement units in eastern AEP (12 installed and 15 additional units planned)
- Monitor the states of the key buses and stations

Operating Condition Generation

- 29 operating conditions are generated in PSAT based on the generation and load patterns provided by the AEP operations staff
- They represent stressed OCs that include the details of load levels, generator outputs and branch power flows during a specific period of time
- The voltages of all the buses in the eastern AEP system are within reasonable levels
 - All the bus voltage magnitudes are adjusted to be between 0.90 and 1.10 p.u.
 - The voltages of 138~765kV buses are adjusted in the range of 0.95~1.10 p.u.

Operating Condition Generation



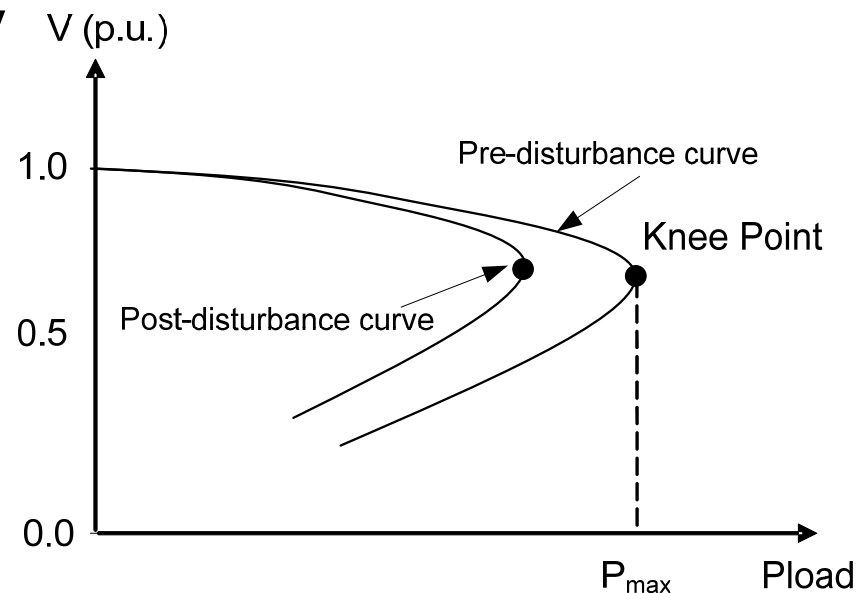
Load Pattern of the 29 Stressed OCs

Voltage Security Evaluation

- A list of contingencies that may cause severe voltage problems is selected according to previous operating experiences in the AEP system
- This list contains 163 N-1 contingencies including different transmission line and transformer outages
- This project adopts a static analysis method to evaluate post-contingency voltage security in VSAT
- A voltage instability judgment is given when a contingency results in the divergence of the power flow solution
- A total number of $29 \times 163 = 4727$ voltage stability simulations are conducted, with either secure or insecure labels marked on each case
- 34.46% of the total cases are insecure

Voltage Stability Criterion

- One commonly used method is the P-V curve method
- The knee point of a P-V curve indicates the maximum power transfer without causing voltage instability
- Further increase in the load over the knee point will cause progressive voltage decline
- Greatly affected by contingency
- A contingency at stressed OCs can cause a power flow solution to diverge



Predictor Selection

- Two main types of predictors, closely related to voltage security problems
- Type 1: Contingency-dependent predictors
 - An unordered bus pair x and y is adopted to denote the faulted branch
 - To eliminate the ordering of the two buses of a critical branch during DT training, each contingency case is doubled in the form of “Bus-1= x and Bus-2= y ” and “Bus-1= y and Bus-2= x ”
 - Allows the DTs to identify buses or substations common to contingencies that are more prone to cause voltage collapse
- Type 2: Pre-contingency system parameters
 - Chosen from the existing PMU measured pre-disturbance system parameters
 - Different types of system variables are collected

Predictor Selection

- 8 groups of predictors are defined, all from the existing PMUs

| No. | Predictors |
|---------|--|
| Group 1 | Faulted bus (FB) and Other bus (OB) of the contingency branch |
| Group 2 | Voltage phase angle differences (A_{x_y}) |
| Group 3 | A_{x_y} , FB, OB |
| Group 4 | Current magnitudes on branches (I_{x_y}), FB, OB |
| Group 5 | MVAr flows on branches (Q_{x_y}), FB, OB |
| Group 6 | Square of voltage magnitudes (V^2_x), FB and OB |
| Group 7 | Absolute value of current magnitude multiplied by branch impedance (IZ_{x_y}), FB and OB |
| Group 8 | A_{x_y} , Q_{x_y} , I_{x_y} , V^2_x , IZ_{x_y} , FB, OB |

Database Example

| SECUS\$ | FB\$ | OB\$ | Q_35_129 | I_4513_4515 | A_35_129 | ... |
|---------|------|------|----------|-------------|----------|----------------|
| S | 1998 | 2266 | -398.5 | 13.4 | 0.9 | |
| S | 2266 | 1998 | -398.5 | 13.4 | 0.9 | |
| I | 5983 | 9319 | -398.5 | 13.4 | 0.9 | |
| I | 9319 | 5983 | -398.5 | 13.4 | 0.9 | for OC1 |
| S | 1205 | 1207 | -398.5 | 13.4 | 0.9 | |
| S | 1207 | 1205 | -398.5 | 13.4 | 0.9 | |
| ... | ... | ... | ... | ... | ... | |
| I | 1998 | 2266 | -410 | 15 | 1.2 | ... |
| I | 2266 | 1998 | -410 | 15 | 1.2 | |
| S | 5983 | 9319 | -410 | 15 | 1.2 | |
| I | 9319 | 5983 | -410 | 15 | 1.2 | for OC2 |
| S | 1205 | 1207 | -410 | 15 | 1.2 | |
| S | 1207 | 1205 | -410 | 15 | 1.2 | |
| ... | ... | ... | ... | ... | ... | ... |

- First column is the predictive objective, secure or insecure
- The other columns represent different predictors defined above
- Each row represents one voltage security simulation case
- For the same OC, the only difference rests with the faulted branch

DT Training and Performance

- All the 9454 cases in the created database are given equal weight
- 1891 cases (20%) are randomly selected to form a test set (TS)
- The cost of misclassifying an insecure case to be a secure case is reasonably increased
- Different algorithms including 'Gini', 'Symmetric Gini', 'Entropy', 'Class Probability', 'Twoing' and 'Ordered Twoing' are tested and compared
- 8 optimal DTs are trained using the above predictor groups

| Opt. DTs | Size | Learning Set Accuracy (%) | | | Test Set Accuracy (%) | | |
|------------|-----------|---------------------------|--------------|--------------|-----------------------|--------------|--------------|
| | | I | S | Overall | I | S | Overall |
| DT1 | 24 | 71.4 | 63.31 | 66.08 | 68.82 | 60.95 | 63.72 |
| DT2 | 7 | 87.61 | 76.99 | 80.63 | 86.96 | 80.07 | 82.50 |
| DT3 | 36 | 98.69 | 94.33 | 95.82 | 91.00 | 93.63 | 92.70 |
| DT4 | 50 | 99.50 | 95.66 | 96.97 | 92.95 | 94.93 | 94.24 |
| DT5 | 31 | 98.11 | 93.89 | 95.33 | 87.11 | 93.3 | 91.12 |
| DT6 | 38 | 96.49 | 92.42 | 93.81 | 88.91 | 91.91 | 90.85 |
| DT7 | 55 | 99.69 | 95.19 | 96.73 | 91.00 | 93.46 | 92.6 |
| DT8 | 51 | 99.11 | 96.00 | 97.06 | 90.55 | 94.44 | 93.07 |

Observations

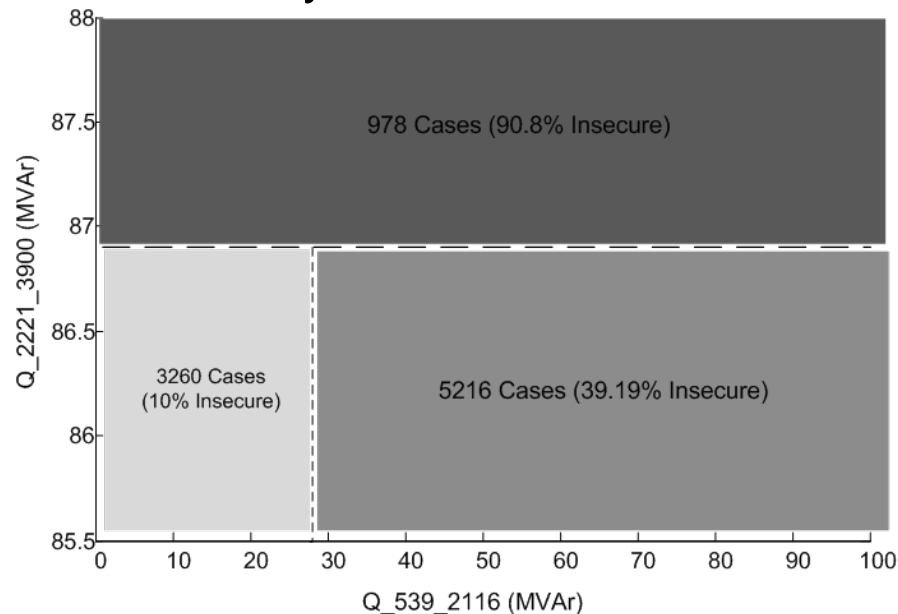
- Pre-contingency parameters are more important than contingency information in voltage security prediction at stressed OCs (DT2 performs much better than DT1)
- The combination of FB, OB and different pre-contingency parameters are helpful for building much better DTs (DT3-DT8)
- A single DT with the highest accuracy on the test set is obtained by using current magnitudes measured by PMUs
- Combining all the predictors did not improve the overall accuracy on the test set
 - Over-fitting problem
 - Predictor masking problem

Efficiency of DTs & Nomogram

- Optimal DTs are very efficient. Only a small number of CSRs are selected in DT3 to DT8

| DTs | Ns/Nt | DTs | Ns/Nt |
|-----|--------|-----|--------|
| DT3 | 15/353 | DT6 | 13/29 |
| DT4 | 16/87 | DT7 | 17/87 |
| DT5 | 12/87 | DT8 | 18/635 |

- Nomogram determined by DT5

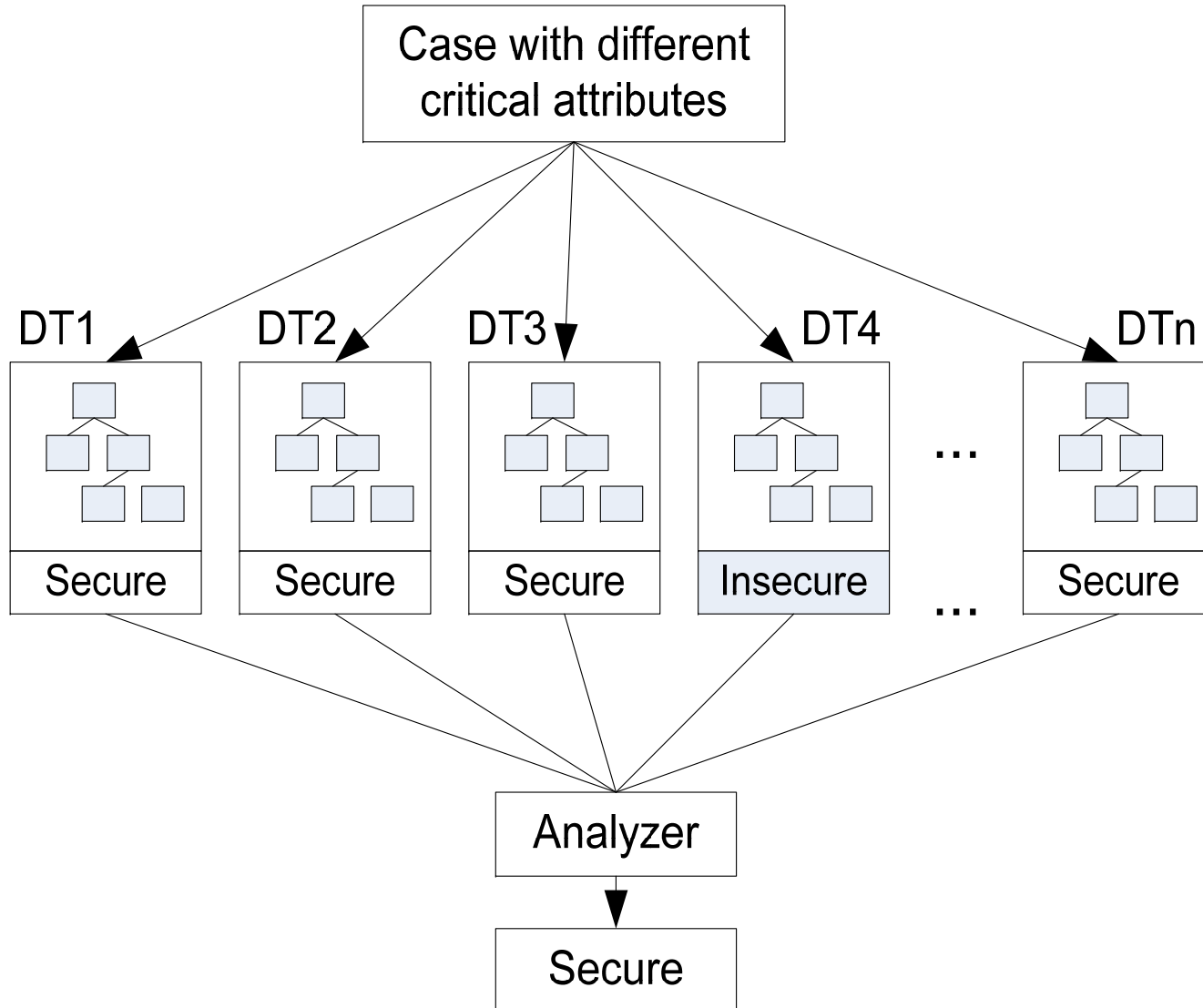


Nomogram in terms of the top two CSRs in DT5

DT Performance Improvement

- Method 1: Multiple DTs
 - Motivation - The combination of all the available predictors may not improve the DT performance on the test set
 - Trusting only one DT has limitations
 - This method takes advantage of all the DTs that satisfy a desired threshold of performance instead of trusting the tree with the best performance only
 - The cases that are misclassified by the best DT may be correctly predicted by the other trees that use different PMU-measured critical attributes.
 - All the optimal DTs are used to obtain a comprehensive classification result

Concept of Multiple DTs



Multiple DTs

- A heuristic search is conducted to identify different combinations of these predictors that contribute to good decision trees
- The multiple DTs that are used for online application should be sufficiently different from each other.
- Certain types of predictors can be totally masked when combined with other predictors, e.g., V^2_x
- 9 DTs with good performance on the TS are obtained by predictor combination
- The result shows most of them offer better prediction performance on the TS than the DTs trained before predictor combination.
- All the 15 (6+9) decision trees from DT3 to DT17 are used for online application since they are capable of correctly predicting over 91% of cases in the TS

Performance of the 9 DTs

DT Performance for Different Predictor Combinations

| Opt. DTs | Size | Predictor combinations | Test Set Accuracy (%) | | |
|----------|------|---------------------------|-----------------------|-------|---------|
| | | | I | S | Overall |
| DT9 | 59 | A_x_y, I_x_y, FB, | 90.4 | 95.59 | 93.76 |
| DT10 | 49 | A_x_y, Q_x_y, FB, | 89.21 | 95.02 | 92.97 |
| DT11 | 47 | A_x_y, IZ_x_y, FB, | 90.85 | 94.12 | 92.97 |
| DT12 | 55 | I_x_y, Q_x_y, FB, | 92.95 | 95.26 | 94.45 |
| DT13 | 45 | Q_x_y, IZ_x_y, FB, | 91.00 | 93.79 | 92.81 |
| DT14 | 53 | A_x_y, I_x_y, Q_x_y, FB, | 92.95 | 95.18 | 94.39 |
| DT15 | 47 | A_x_y, I_x_y, IZ_x_y, FB, | 90.85 | 94.12 | 92.97 |
| DT16 | 53 | I_x_y, Q_x_y, IZ_x_y, FB, | 91.15 | 93.14 | 92.44 |
| DT17 | 45 | A_x_y, Q_x_y, IZ_x_y, FB, | 91.00 | 93.79 | 92.81 |

Performance Using the 15 DTs

- For any contingency case, 15 voltage stability assessments are obtained separately and a final assessment is given in terms of the majority classification result, either secure or insecure
- A statistical analysis is conducted on the 1891 cases in the TS and 7563 cases in the LS using these 15 DT models
- The overall prediction accuracy on the TS is increased to 94.66%; while the accuracy on the LS is increased to 97.75%
- Using multiple DTs in real time will not cause a significant increase in the security assessment time
- The DTs are all trained offline and the assessment process using different DTs can be conducted individually

DT Performance Improvement

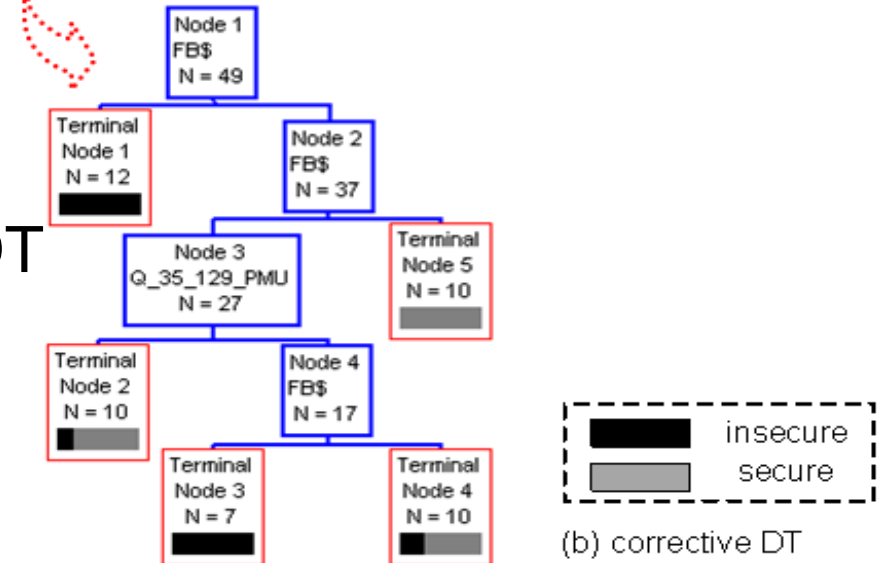
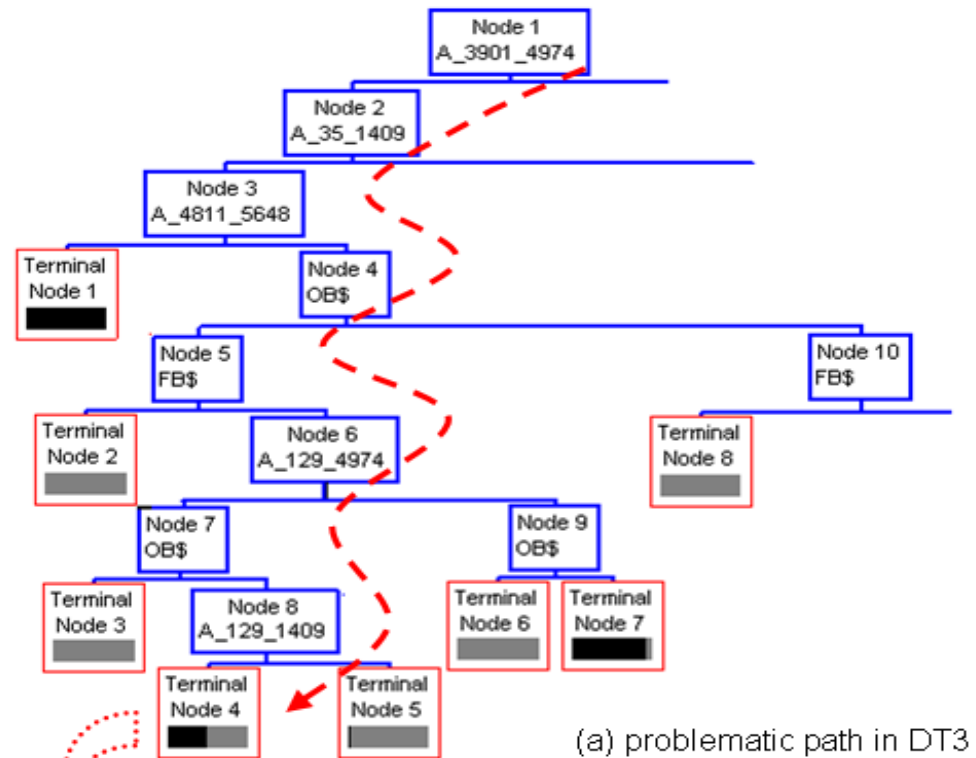
- Method 2: Corrective DTs
 - An important observation from the trained DTs is that most of the paths in a single DT trained by only one type of pre-contingency parameter (e.g. DT3) have excellent prediction behavior
 - Only a few paths have severe misclassification problems
 - Idea: to replace the problematic paths with corrective DTs for accuracy improvement
 - For each of the paths with poor performance, a corrective DT is trained by including more system information for all the cases that fall into this path in the original database
 - For example, a path with poor performance in DT3 is taken to explain how this method works

Corrective DTs

- Focusing on Terminal Node 4
 - 49 cases in the LS
(24 cases are misclassified)
 - 14 cases in the TS
(6 cases are misclassified)

- Train one corrective DT by including more predictors

- Performance of the corrective DT
 - 5 cases misclassified in LS'
 - 3 cases misclassified in TS'



Corrective DTs

- This approach preserves the branches with high accuracy
- It only modifies the paths with severe misclassification problems
- The improved DT performance

| Opt. DTs | Overall LS Accuracy (%) | | Overall TS Accuracy (%) | |
|----------|-------------------------|----------|-------------------------|----------|
| | Corrected | Original | Corrected | Original |
| DT3' | 97.46 | 95.82 | 94.02 | 92.70 |
| DT4' | 98.21 | 96.97 | 95.45 | 94.24 |
| DT5' | 98.70 | 95.33 | 92.07 | 91.12 |
| DT6' | 97.38 | 93.81 | 93.39 | 90.85 |
| DT7' | 98.40 | 96.73 | 93.92 | 92.6 |

Conclusions

- An online voltage security assessment scheme using PMUs and DTs is proposed
- This scheme is tested on the AEP power system
- Properly trained DTs perform well in predicting post-contingency voltage security
- DTs can identify key system parameters as voltage security indicators and provide operators effective nomograms
- Two new methods to improve DT performance are introduced, including “Multiple DTs” and “Corrective DTs”

Publication

- R. Diao, K. Sun, V. Vittal, R. O’Keefe, M. Richardson, N. Bhatt, D. Stratford, and S. Sarawagi, “Decision Tree Based Online Voltage Security Assessment Using PMU Measurements,” Paper accepted for publication in the IEEE Transactions on Power Systems (December 2008).



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THANK YOU!

Questions?