

# Power System State Estimation and Optimal Measurement Placement for Distributed Multi-Utility Operation

Final Project Report

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# Power System State Estimation and Optimal Measurement Placement for Distributed Multi-Utility Operation

**Final Project Report** 

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#### **EXECUTIVE SUMMARY**

The new power markets induce changes in the way the transmission grid is operated and, as a result, an increased number of power transactions take place creating unanticipated power flows through the system. Monitoring these flows reliably and accurately requires a robust measurement system. Furthermore, unlike conventional systems, modern power systems are equipped with advanced power flow controllers or flexible A.C. transmission system (FACTS) devices for redirecting power flows to handle congestion. Monitoring these devices and their parameters is also becoming important. Finally, existence of multiple ISOs/RTOs, and associated inter-utility power exchanges, presents a need for addressing the multi-utility data exchange issues in the new power market environment. Accordingly, the project is divided into two parts. The first part is on the meter placement while the second part focuses on the distributed state estimator for multi-utility data exchanges.

For the first part, a systematic method is developed for placing meters either to upgrade an existing measurement system or to build one from scratch. This method not only ensures observability of the system for a base case operating topology, but also accounts for expected contingencies and measurement losses. In order to address the issue of FACTS devices, a new estimator is developed. This estimator is capable of incorporating the power flow controllers, along with their operating and parameter limits, into the state estimation formulation.

For the second part, we are focusing on the following scenario.

With power market deregulation, member companies cooperate to share one whole grid system and try to achieve their own economic goals. The companies release operational control of their transmission grids to form ISOs/RTOs while maintaining their own state estimators over their own areas.

This project also focuses on how to improve the state estimation result of member companies or the ISO by exchanging raw or estimated data with neighboring member companies (or ISOs). Numerical tests verify that selected data exchange improves the estimator quality of individual entities for both estimation reliability and estimation accuracy. It is also shown that

the benefit of alternative data exchange schemes can be quite different; some data exchanges are even harmful if our principles are not carefully followed.

Another recent trend for these ISOs/RTOs is to combine and grow to form a Mega-RTO grid for a better market efficiency. The determination of state over the whole system becomes challenging due to its large size. Instead of a totally new estimator over the whole grid, we propose a distributed textured algorithm to determine the whole state; in our algorithm, the existing state estimators in local companies/ISOs/RTOs are fully utilized and the new estimator is no longer required. We need only some extra communication for some instrumentation or estimated data exchange. Detailed numerical tests are given to verify the efficiency and validity of the new approach.

The developed methods of this project are implemented in the form of prototype software. Simulations were carried out on test systems and the results are provided in this report.

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# PART I: STATE ESTIMATION OF POWER SYSTEMS EMBEDDED WITH FACTS DEVICES

#### I. INTRODUCTION

#### 1.1 Introduction

After the establishment of power markets with transmission open access, the significance and use of FACTS devices for manipulating line power flows to relieve congestion and optimize the overall grid operation have increased. As a result, there is a need to integrate the FACTS device models into the existing power system applications. This report will present an algorithm for state estimation of network embedded with FACTS devices. Furthermore, it will be shown via case studies that the same estimation program can also be used for determining the controller setting for a desired operating condition.

There are several kinds of FACTS devices. Thyristor-switched series capacitors (TCSC) and thyristor-switched phase shifting transformer (TCPST) can exert a voltage in series with the line and, therefore, can control the active power through a transmission line [3]. On the other hand, the Unified Power Flow Controller (UPFC) has a series voltage source and a shunt voltage source, allowing independent control of the voltage magnitude, and the real and reactive power flows along a given transmission line [1,2]. In this report, only one device, namely the UPFC, will be considered due to its complexity and versatility in controlling power flows.

#### 1.2 Problem Statement

Flexible A.C. transmission systems [FACTS] are being used more in large power systems for their significance in manipulating line power flows. Traditional state estimation methods without integrating FACTS devices will not be suitable for power systems embedded with FACTS.

State estimation in power system can be formulated as a nonlinear weighted least squares (WLS) problem. It has a set of measurement equations:  $z = h(x) + \varepsilon$ ; a set of equality constraints c(x) = 0, representing the zero injections of buses and the zero active power exchange between

the power system and FACTS devices; a set of inequality constraints  $f(x) \le s$ , representing the Var limits on generators, transformer tap ratio limits, and the power and voltage limit of FACTS devices.

This report will present an algorithm to solve this nonlinear weighted least squares problem. By solving the problem we can not only estimate the state variables (bus voltages and phase angles) of power system, but can also determine the controller settings of FACTS devices for a desired operating condition.

In this report, an approach that incorporates FACTS devices into the state estimation will be presented. First, a steady-state model of the UPFC [1,2] with operating and parameters limits will be introduced. Then, the commonly used Hatchtel's augmented matrix method [3,4] will be used to implement a numerically robust and computationally efficient state estimator, which is also flexible enough to account for various device constraints. To treat the inequality constraints, we will introduce the Logarithmic barrier function method [5] and integrate it into Hatchtel's matrix. Simulation results for typical systems are shown at the end of part one. It will be shown via case studies that this program can also be used for determining the controller settings of a UPFC for a desired operating condition.

#### II. PROPOSED ALGORITHM

#### 2.1 Steady state model of UPFC

The Unified Power Flow Controller (UPFC) [1,2] can control the voltage magnitude, real and reactive power flows simultaneously. The real physical model of UPFC consists of two switching converters as illustrated in Figure 1.1. These inverters are operated from a common dc link provided by a dc storage capacitor. This arrangement functions as an ideal ac to ac power converter in which the real power can freely flow in either direction between the ac terminals of the two inverters and each inverter can independently generate (or absorb) reactive power at its own ac output terminal [2].

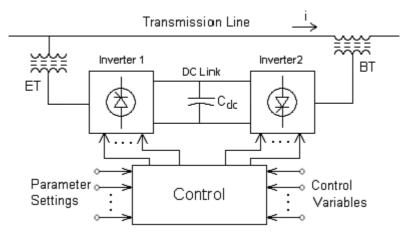


Fig. 1.1 Basic circuit arrangement of the Unified Power Flow Controller

The steady state model of UPFC consists of two ideal voltage sources, one in series and one in parallel with the associated line, as shown in Figure 1.2. Neglecting UPFC losses, during steady-state operation it neither absorbs nor injects real power into the system [2].

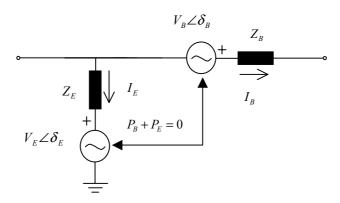


Fig. 1.2 Steady state model of UPFC

The constraint  $P_B + P_E = 0$  in Figure 1.2 has two implications.

No real-power is exchanged between the UPFC and the system.

The two sources are mutually dependent.

The real and reactive power going through line k-m can be formulated by equations (1.1) to (1.4).

$$P_{km} = \frac{|V_k||V_m|}{X_B} \sin \theta_{km} + \frac{|V_k||V_E|}{X_E} \sin \theta_{k,E} - \frac{|V_k||V_B|}{X_B} \sin \theta_{k,B}$$
(1.1)

$$Q_{km} = \frac{X_E + X_E}{X_B X_E} |V_k|^2 - \frac{|V_k| V_m|}{X_B} \cos \theta_{km} - \frac{|V_k| V_E|}{X_E} \cos \theta_{k,E} + \frac{|V_k| V_B|}{X_B} \cos \theta_{k,B}$$
(1.2)

$$P_{mk} = \frac{|V_k||V_m|}{X_B} \sin \theta_{mk} + \frac{|V_m||V_B|}{X_B} \sin \theta_{m,B}$$
 (1.3)

$$Q_{mk} = \frac{|V_m|^2}{X_B} - \frac{|V_k||V_m|}{X_B} \cos \theta_{mk} - \frac{|V_m||V_B|}{X_B} \cos \theta_{m,B}$$
 (1.4)

Variables  $V_E$ ,  $\theta_E$ ,  $V_B$ ,  $\theta_B$  are the control parameters of the UPFC. There are equality and inequality constraints for the UPFC, which can be formulated by equations (1.5) to (1.9).

Real Power Constraints: 
$$P_E + P_B = 0$$
 (1.5)

Shunt Power Constraints: 
$$\sqrt{P_E^2 + Q_E^2} \le T_{E,\text{max}}$$
 (1.6)

Series Power Constraints: 
$$\left| \sqrt{P_B^2 + Q_B^2} \right| \le T_{B,\text{max}}$$
 (1.7)

Shunt Voltage Constraints: 
$$|V_B| \le V_{B,\text{max}}$$
 (1.8)

Series Voltage Constraints: 
$$|V_E| \le V_{E \text{ max}}$$
 (1.9)

#### 2.2 HACHTEL's augmented matrix method [3,4]

Power system state estimation problem can be formulated as a nonlinear least squares problem with a set of equality and inequality constraints [6].

Min 
$$\frac{1}{2}r^{T}R^{-1}r$$

$$f(x)+s = 0$$

$$c(x) = 0$$
s.t. 
$$r-z+h(x)=0$$

$$s \ge 0$$

$$(1.10)$$

z = h(x) + r represents the equations for measurements, where z is the (mx1) measurement vector, h(.) is the (mx1) vector of nonlinear functions, "x" is the (nx1) state vector, "r" is the (mx1) measurement error vector.

c(x) = 0 represents the equality constraints, where  $c(\cdot)$  is the  $(r \times 1)$  vector of nonlinear functions. These equality constraints represent the zero injection buses and the zero active power exchange between the system and the FACTS devices.

 $f(x) \leq 0$  represents the inequality constraints, which represent the Var limits on generators, ratio limits of transformer taps, and the power and voltage limits of the UPFC  $(\sqrt{P_E^2 + Q_E^2} \leq T_{E,\text{max}}, \left| \sqrt{P_B^2 + Q_B^2} \right| \leq T_{B,\text{max}}, \left| V_B \right| \leq V_{B,\text{max}}, \left| V_E \right| \leq V_{E,\text{max}}).$ 

s is a vector of slack variables used to convert the inequality constraints to equality constraints.

In order to solve the problem of (1.10), we will employ the interior point optimization method. In this method, the slack variables are treated by appending a logarithmic barrier function to the objective function,

$$\phi_{\mu} = \frac{1}{2} r^{T} R^{-1} r - \mu \sum_{k=1}^{p} \ln s_{k}$$
 (1.11)

where p is the number of inequality constraints and  $s_k$  is the kth element of the slack variable vector s. The barrier parameter  $\mu > 0$  is forced to decrease towards zero as the iterations progress.

The Lagrangian function is given by (1.12).

$$L_{\mu} = \frac{1}{2} r^{T} R^{-1} r - \mu \sum_{k=1}^{p} \ln s_{k} - \lambda^{T} [f(x) + s] - \rho^{T} g(x) - \pi^{T} [r - z + h(x)]$$
 (1.12)

By using the Kuhn-Karroush-Tucker (KKT) optimality conditions and replacing the nonlinear functions by their first order approximations, the solution to the nonlinear least squares problem will be obtained by iteratively solving the following linear equations:

$$\begin{bmatrix} D & 0 & 0 & F \\ 0 & 0 & 0 & G \\ 0 & 0 & R & H \\ F^{T} & G^{T} & H^{T} & 0 \end{bmatrix} \cdot \begin{bmatrix} \lambda \\ \rho \\ \pi \\ \Delta x \end{bmatrix} = \begin{bmatrix} -f(x^{k}) \\ -g(x^{k}) \\ z - h(x^{k}) \\ 0 \end{bmatrix}$$
(1.13)

The matrix on the left side will be referred as the K matrix. Matrices F, G, H are the gradient matrices of the functions f(x), g(x), h(x) respectively. D is built as (1.14), where S is the diagonal matrix whose  $k^{th}$  diagonal element is  $s_k$ .

$$D = \frac{1}{\mu}(S)^2 \tag{1.14}$$

Solving (1.13) iteratively yields the solution for (1.10).

#### 2.3 Observability Analysis

Observability analysis can be carried out using the numerical method. The Jacobian

Peter-Wilkinson method. In the case of zero pivots, pseudo-measurements will be added to make the system observable. The pseudo-measurements will indicate deficiencies in the measurement system, both for the network states as well as for the FACTS device parameters.

#### 2.4 Equations

This section provides the detailed equations for the measurements incident to a given line, both with and without a UPFC device.

#### 2.4.1 Lines without an installed UPFC

Consider two possible measurements (1 and 2) on line k-m.

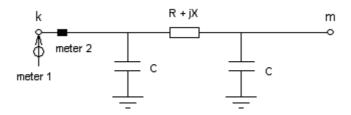


Fig. 1.3 Candidate measurements on line k-m without UPFC

Equations for meter 1 are:

$$P_{k} = V_{k}^{2} G_{kk} + V_{k} \sum_{j=1, j \neq k}^{n} V_{j} (G_{kj} \cos \theta_{kj} + B_{kj} \sin \theta_{kj})$$
(1.15)

$$Q_k = -V_k^2 B_{kk} + V_k \sum_{j=1, j \neq k}^n V_j (G_{kj} \sin \theta_{kj} - B_{kj} \cos \theta_{kj})$$
(1.16)

Equations for meter 2 are:

$$P_{k} = -V_{k}^{2} G_{km} + V_{k} V_{m} (G_{km} \cos \theta_{km} + B_{km} \sin \theta_{km})$$
(1.17)

$$Q_k = V_k^2 (B_{km} - C_{km}) + V_k V_m (G_{km} \sin \theta_{km} - B_{km} \cos \theta_{km})$$
(1.18)

#### 2.4.2 Lines controlled by a UPFC

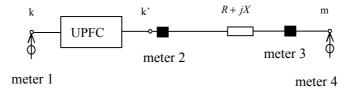


Fig. 1.4 UPFC and candidate measurements on line k-m

Suppose a UPFC is installed on line k-m. Measurements 1, 2, 3, 4 are the measurements that can be placed on line k-m.

Equations for meter 1 are:

$$P_{k} = V_{k}^{2} (G_{kk} + G_{km}) + V_{k} \sum_{\substack{j=1\\j \neq k,m}}^{n} V_{j} (G_{kj} \cos \theta_{kj} + B_{kj} \sin \theta_{kj})$$

$$+ V_{k} V_{B} B_{B} \sin \theta_{kB} - V_{k} V_{k} B_{B} \sin \theta_{kk'} - V_{k} V_{E} B_{E} \sin \theta_{kE}$$

$$(1.19)$$

$$Q_{k} = -V_{k}^{2}(B_{kk} + B_{km} + B_{B} + B_{E}) + V_{k} \sum_{\substack{j=1\\j \neq k,m}}^{n} V_{j}(G_{kj} \sin \theta_{kj} - B_{kj} \cos \theta_{kj})$$

$$-V_{k}V_{B}B_{B} \cos \theta_{kB} + V_{k}V_{k}B_{B} \cos \theta_{kk} + V_{k}V_{E}B_{E} \cos \theta_{kE}$$
(1.20)

Equations for meter 2 are:

$$P_{km} = V_{k'}V_k B_B \sin \theta_{k'k} + V_{k'}V_B B_B \sin \theta_{k'B} \tag{1.21}$$

$$Q_{km} = V_{k'}^2 B_B - V_{k'} V_k B_B \cos \theta_{k'k} - V_{k'} V_B B_B \cos \theta_{k'B}$$
 (1.22)

and

$$P_{km} = -V_{k'}^2 G_{km} + V_{k'} V_m (G_{km} \cos \theta_{k'm} + B_{km} \sin \theta_{k'm})$$
(1.23)

$$Q_{km} = V_{k'}^{2} (B_{km} - C_{km0}) + V_{k'} V_{m} (G_{km} \sin \theta_{k'm} - B_{km} \cos \theta_{k'm})$$
(1.24)

Equations for meter 3 are:

$$P_{mk} = -V_m^2 G_{km}^{'} + V_m V_k (G_{kj} \cos \theta_{mkj} + B_{kj} \sin \theta_{mk}) + V_m V_R (G_{km}^{'} \cos \theta_{mR} + B_{km}^{'} \sin \theta_{mR})$$
(1.25)

$$Q_{mk} = V_m^2 (B_{km}^{'} - C_{mk0}) + V_m V_k (G_{kj} \sin \theta_{mkj} - B_{kj} \cos \theta_{mk}) + V_m V_B (G_{km}^{'} \sin \theta_{mB} - B_{km}^{'} \cos \theta_{mB})$$
(1.26)

Equations for meter 4 are:

$$P_{m} = V_{m}^{2} (G_{mm} + G_{mk} - G_{km}^{'}) + V_{m} \sum_{\substack{j=1\\j \neq k,m}}^{n} V_{j} (G_{mj} \cos \theta_{mj} + B_{mj} \sin \theta_{mj})$$

$$+ V_{m} V_{k} (G_{km}^{'} \cos \theta_{mk} + B_{km}^{'} \sin \theta_{mk}) + V_{m} V_{B} (G_{km}^{'} \cos \theta_{mB} + B_{km}^{'} \sin \theta_{mB})$$

$$(1.27)$$

$$Q_{m} = -V_{m}^{2}(B_{mm} + B_{mk} - B_{km}^{'}) + V_{m} \sum_{\substack{j=1\\j \neq k,m}}^{n} V_{j}(G_{mj} \sin \theta_{mj} - B_{mj} \cos \theta_{mj})$$

$$+V_{m}V_{k}(G_{km}^{'} \sin \theta_{mk} - B_{km}^{'} \cos \theta_{mk}) + V_{m}V_{B}(G_{km}^{'} \sin \theta_{mB} - B_{km}^{'} \cos \theta_{mB})$$

$$(1.28)$$

#### 2.5 Algorithm

The following algorithm is used in this program of state estimation. It is based upon the previously presented analysis and the reader is referred to the previous sections for the notation used in the following description of algorithm steps.

**Step 1:** Read network data and measurements.

**Step 2:** Initialize:  $x^{(k)}$ , k = 0.

**Step 3:** Form  $K^{(k)}$  matrix.

Step 4: Calculate the equality and inequality constraints, measurements mismatch, and form

the right hand side b vector. 
$$b^{(k)} = \begin{bmatrix} -f(x^k) \\ -g(x^k) \\ z - h(x^k) \\ 0 \end{bmatrix}.$$

Step 5: Solve the equation: 
$$K^{(k)} \cdot \begin{bmatrix} \lambda \\ \rho \\ \pi \\ \Delta x \end{bmatrix} = b^{(k)}$$
, get  $\Delta x^{(k)}$ .

**Step 6:** Update  $x: x^{(k+1)} = x^{(k)} + \Delta x^{(k)}$ .

**Step 7:** Terminate execution if  $\Delta x^{(k)} - \Delta x^{(k-1)} \le \mathcal{E}$ , and go to **step 8**, else, k = k+1 and go to step 3.

**Step 8:** Stop and print out results.

#### III. NUMERICAL EXAMPLES

#### **3.1 14-bus system**

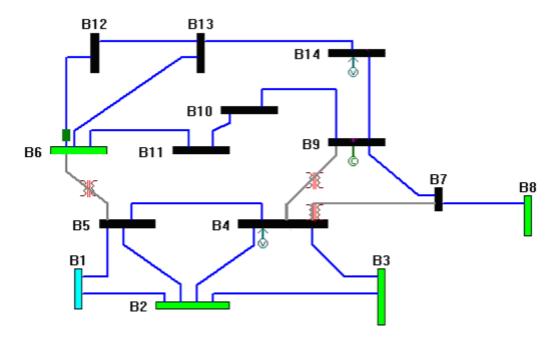


Fig. 1.5 IEEE-14 system

IEEE-14 bus system is shown in Figure 1.5. A FACTS device (UPFC) is installed on line 6-12, near bus 6. The parameters of UPFC are shown below.

#### Parameters of the installed UPFC device:

From (bus)	To (bus)	$X_{\scriptscriptstyle B}$	$X_{\scriptscriptstyle E}$	$V_{B,\max}$	$V_{E,\mathrm{max}}$	$S_{B,\max}$	$S_{E,\mathrm{max}}$
6	12	0.7	0.7	1.0	1.0	1.0	1.0

The developed program can be utilized in two different ways depending upon the purpose of the study. It can be used as an estimator of the FACTS device parameters for a given set of measurements. The estimation will yield not only the system states but also the FACTS device parameters. It can also be utilized as a tool to estimate the required values for the parameters of the FACTS devices in order to maintain a specific level of flow through a specified line. The amount of desired power flow through line 6-12, which happens to have a FACTS device installed on it, can be maintained by the use of this program and estimating the required settings of the control variables of this FACTS device.

First, the function of the program as an estimator will be illustrated.

Suppose that the system has voltage magnitude, bus injection and line flow measurements. The measurement values are shown below.

#### Voltage Measurements:

Bus No.	Voltage	Bus No.	Voltage
4	1.01870	14	1.03700

#### Bus Injection Measurements:

Bus No.	P	Q	Bus No.	P	Q
3	-0.94200	0.04393	5	-0.07600	0.01600
6	-0.11200	0.04718	7	0.00000	0.00000
8	0.00000	0.17357	9	-0.29500	-0.16600
10	-0.09000	-0.05800	11	-0.03500	-0.01800
13	-0.13500	-0.05800			

#### Line Flow Measurements:

Bus No. (From)	Bus No. (To)	Active Power P	Reactive Power Q
1	2	1.56771	-0.20378
2	3	0.73161	0.03568
4	7	0.27870	-0.09478
9	14	0.08801	0.03591
6	13	0.13670	0.07187
6	12	0.12464	0.02372

The program is executed and all the unknown state and control variables of the UPFC device are estimated.

The state estimation results are shown below:

#### State variables:

Bus No.	V	$\theta$ (Degree)	Bus No.	V	$\theta$ (Degree)
1	1.059985	0	2	1.044985	-4.979034
3	1.009984	-12.713291	4	1.018685	-10.318546
5	1.020265	-8.783118	6	1.069983	-14.261062
7	1.062103	-13.338571	8	1.089985	-13.338488
9	1.056632	-14.904211	10	1.051579	-15.076087
11	1.057220	-14.799891	12	1.067199	-14.363372
13	1.052852	-14.924974	14	1.037014	-15.909763

Voltages and powers of FACTS device:

V <sub>B</sub>	$P_{\scriptscriptstyle B}$	$S_{\scriptscriptstyle B}$	$\stackrel{\cdot}{V}_{E}$	$P_{\scriptscriptstyle E}$	$S_{\scriptscriptstyle E}$
0.1099∠60.0695°	0.0014	0.0128	$1.0679 \angle -14.3099^{\circ}$	-0.0014	0.0035

Note that  $P_B + P_E = 0$  and  $V_B \le 1.0$ ,  $S_B \le 1.0$ ,  $V_E \le 1.0$ ,  $S_E \le 1.0$ , which correctly satisfy all the constraints.

The estimated and actual values for each measurement are given below.

Bus Type	Bus No.1	Bus No.2	Real Value	Estimated Value
Volta an matama	4		1.0187	1.0187
Voltage meters	14		1.0370	1.0370
	11		-0.0350 – j 0.0180	-0.0350 – j 0.0180
	10		-0.0900 – j 0.0580	-0.0900 – j 0.0580
Injection meters	5		-0.0760 – j 0.0160	-0.0760 – j 0.0160
	6		-001120 + j 0.0470	-001120 + j 0.0470
	13		-0.1350 – j 0.0580	-0.1350 – j 0.0580
	8		0.0000 + j 0.1725	0.0000 + j 0.1725
	7		0.0000 + j 0.0000	0.0000 + j 0.0000
	9		-0.2950 – j 0.1660	-0.2950 – j 0.1660
	3		-0.8420 + j 0.0435	-0.8420 + j 0.0435
	6	12	0.1246 + j 0.0237	0.1246 + j 0.0237
	1	2	1.5677 – j 0.2038	1.5677 – j 0.2038
Flow meters	2	3	0.7316 + j 0.0357	0.7316 + j 0.0357
Flow meters	4	7	0.2787 – j 0.0948	0.2787 – j 0.0948
	9	14	0.0880 + j 0.0359	0.0880 + j 0.0359
	6	13	0.1367 + j 0.0719	0.1367 + j 0.0719

Next, the program's usage as a power flow controller will be illustrated. Consider a case where the power flow data (with bus 1 chosen as slack with a voltage magnitude of 1.06) are given as below.

Bus No.	P	Q	Bus No.	P	Q
2	0.18300	0.29695	3	-0.94200	0.04393
4	0.47800	0.03900	5	-0.07600	0.01600
6	-0.11200	0.04718	7	0.00000	0.00000
8	0.00000	0.17357	9	-0.29500	-0.16600
10	-0.09000	-0.05800	11	-0.03500	-0.01800
12	-0.06100	-0.01600	13	-0.13500	-0.05800
14	-0.14900	-0.05000			

First the state of the system with fixed UPFC parameters is estimated. The resulting system state and the power flow through the line 6-12 are given below.

#### State variables:

Bus No.	V	$\theta$ (Degree)	Bus No.	V	$\theta$ (Degree)
1	1.060000	0	2	1.044993	-4.980830
3	1.009988	-12.717979	4	1.018608	-10.324100
5	1.020248	-8.782366	6	1.069953	-14.222568
7	1.061927	-13.368356	8	1.089978	-13.368356
9	1.056318	-14.946878	10	1.051296	-15.104578
11	1.057042	-14.795379	12	1.055177	-15.077467
13	1.050399	-15.159014	14	1.035760	-16.039228

#### Power flow in branch 6-12:

Bus No. (From)	Bus No. (To)	$P_{6-12} + jQ_{6-12}$
6	12	0.007780 + j 0.02487

Then, the UPFC model is incorporated into the state estimation formulation. In this case, the system is underspecified and, hence, an extra equation is needed. This equation will be provided by the power flow measurement which will now be set equal to the desired value of the flow through the device in branch 6-12, which, in this example, is set equal to 0.1 + j0.1, leaving all the other conditions the same.

The estimated state variables in this case are:

Bus No.	V	$\theta$ (Degree)	Bus No.	V	$\theta$ (Degree)
1	1.060000	0	2	1.041468	-4.969482
3	1.004075	-12.779670	4	1.010975	-10.340952
5	1.012474	-8.766850	6	1.047481	-14.387390
7	1.051088	-13.499823	8	1.079413	-13.499823
9	1.043792	-15.145037	10	1.036937	-15.311199
11	1.038676	-14.992481	12	1.061751	-15.763135
13	1.037873	-15.383072	14	1.023009	-16.273076

Control variables and estimated power of the FACTS device are:

V <sub>B</sub>	$P_{\scriptscriptstyle B}$	$S_{\scriptscriptstyle B}$	V <sub>E</sub>	$P_E$	$S_E$
0.1236∠9.0530°	0.0056	0.0159	1.0000∠-14.6037°	-0.0056	0.0681

Note again that,  $P_B + P_E = 0$ , and  $V_B \le 1.0$ ,  $S_B \le 1.0$ ,  $V_E = 1.0$ ,  $S_E \le 1.0$ , which satisfy all the constraints.

Now the power flow in branch 6-12 is 0.1009 + j0.0999, which closely matches the desired set values, the slight difference possibly being due to the fact that the upper limit of  $V_E$  is reached at the optimal solution.

This example illustrates that by setting the control variables of UPFC to  $V_B = 0.1236 \angle 9.0530^\circ$  and  $V_E = 1.0000 \angle -14.6037^\circ$ , the power flow in branch 6-12 can be maintained at the desired amount.

#### 3.2 30-bus system

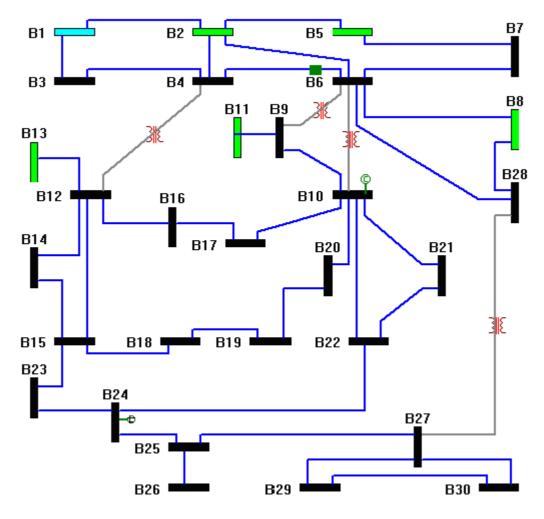


Fig. 1.6 IEEE-30 system

IEEE-30 bus system is shown in Figure 1.6. A FACTS device (UPFC) is installed on line 4-6, near bus 6. The parameters of FACTS device are shown below.

Parameters of the installed UPFC device:

From (bus)	To (bus)	$X_{\scriptscriptstyle B}$	$X_{\scriptscriptstyle E}$	$V_{B,\max}$	$V_{E,\max}$	$S_{B,\max}$	$S_{E,\mathrm{max}}$
6	4	0.7	0.7	1.1	1.1	1.0	1.0

First, the function of the program as an estimator will be illustrated.

Suppose that the system has bus injection measurements and line flow measurements. The measurement values are shown as below. Bus 1 is the assumed slack bus with a specified voltage magnitude of 1.06.

## Injection Meters:

Bus No.	P	Q	Bus No.	Р	Q
1	2.60137	-0.15420	2	0.18300	0.35540
3	-0.02400	-0.01200	5	-0.94200	0.17612
8	-0.30000	0.05226	9	0.00000	0.00000
10	-0.05800	-0.02000	13	0.00000	0.11163
12	-0.11200	0.11163	15	-0.08200	-0.02500
21	-0.17500	-0.11200	27	0.00000	0.00000
24	-0.08700	-0.06700	26	-0.03500	-0.02300
4	-0.07600	-0.01600	6	0.00000	0.00000

### Flow Meters:

Bus No. (From)	Bus No. (To)	Active Power P	Reactive Power Q
1	2	1.68682	-0.20029
1	3	0.91576	0.04609
2	5	0.79259	0.02011
2	6	0.53422	0.01609
9	11	0.00000	-0.15412
13	12	0.00000	0.11163
12	16	0.05434	0.03611
14	15	0.01197	0.00809
16	17	0.01899	0.01736
15	18	0.05074	0.01838
18	19	0.01846	0.00879
10	21	0.16017	0.09975
15	23	0.04012	0.03217
22	24	0.06118	0.02992
25	26	0.03542	0.02364
25	27	-0.05405	-0.00118
28	27	0.18718	0.04882
29	30	0.03704	0.00607
6	28	0.19201	0.00122
6	4	-0.84823	0.18578

The program is executed and all the unknown state and control variables of the UPFC device are estimated.

The state estimate results are shown below:

#### State variables:

Bus No.	V	$\theta$ (Degree)	Bus No.	V	$\theta$ (Degree)
1	1.060000	0	2	1.043158	-5.278306
3	1.019352	-8.553746	4	1.010265	-10.311362
5	1.010131	-13.591051	6	1.012456	-10.248681
7	1.002980	-11.973942	8	1.011528	-10.986111
9	1.055265	-13.708757	10	1.051314	-15.510934
11	1.085641	-13.706705	12	1.063071	-15.517050
13	1.077737	-15.520280	14	1.050847	-16.441173
15	1.045770	-16.406170	16	1.051925	-15.917530
17	1.047809	-16.060072	18	1.037281	-16.906830
19	1.035051	-17.004135	20	1.032174	-16.056766
21	1.038988	-15.963820	22	1.039526	-15.955809
23	1.035933	-16.655654	24	1.027863	-16.395538
25	1.021634	-15.606883	26	1.003342	-15.943536
27	1.026629	-14.899834	28	1.008883	-10.891553
29	1.005645	-16.036445	30	0.994189	-16.915230

#### Voltages and power of FACTS device:

$\overset{\cdot}{V}_{B}$	$P_{\scriptscriptstyle B}$	$S_{\scriptscriptstyle B}$	V <sub>E</sub>	$P_{\scriptscriptstyle E}$	$S_{\scriptscriptstyle E}$
0.2089∠-93.6960°	0.0106	0.1797	1.0077∠-10.3676°	-0.0106	0.0264

Note that  $P_B + P_E = 0$  and  $V_B \le 1.1$ ,  $S_B \le 1.0$ ,  $V_E \le 1.1$ ,  $S_E \le 1.0$ , which correctly satisfy all the constraints.

The estimated and actual values for each measurement are given below.

Bus Type	Bus No.1	Bus No.2	Real Value	Estimated Value
	1		2.6014 – j 0.1542	2.6058 – j 0.1580
	2		0.1830 + j 0.3554	0.1713 + j 0.3568
	3		-0.0240 – j 0.0120	-0.0155 – j 0.0189
	5		-0.9420 + j 0.1761	-0.9412 + j 0.1760
	8		-0.3000 + j 0.0523	-0.3007 + j 0.0523
	9		0 + j 0	0 + j 0
	10		-0.0580 – j 0.0200	-0.0580 – j 0.0200
Injection meters	13		0.0000 + j 0.1116	0.0005 + j 0.1104
injection meters	12		-0.1120 – j 0.0750	-0.1111 – j 0.0776
	15		-0.0820 – j 0.0250	-0.0816 – j 0.0277
	21		-0.1750 – j 0.1120	-0.1755 – j 0.1113
	27		0 + j 0	-0.0000 – j 0.0000
	24		-0.0870 – j 0.0670	-0.0890 – j 0.0641
	26		-0.0350 – j 0.0230	-0.0367 – j 0.0200
	4		-0.0760 – j 0.0160	-0.0721 – j 0.0196
	6		0 + j 0	0 + j 0

Next the program's usage as a power flow controller will be illustrated. Consider a case where the power flow data (where bus 1 is chosen as slack with a voltage magnitude of 1.06) are given as below.

Bus No.	P	Q	Bus No.	P	Q
2	0.18300	0.31635	3	-0.024	-0.01200
4	-0.07600	-0.01600	5	-0.94200	0.16763
6	0.00000	0.00000	7	-0.22800	-0.10900
8	-0.30000	0.01710	9	0.00000	0.00000
10	-0.05800	-0.02000	11	0.00000	0.24000
12	-0.11200	-0.07500	13	0.00000	0.24000
14	-0.06200	-0.01600	15	-0.08200	-0.02500
16	-0.03500	-0.01800	17	-0.09000	-0.05800
18	-0.03200	-0.00900	19	-0.09500	-0.03400
20	-0.02200	-0.00700	21	-0.17500	-0.11200
22	0.00000	0.00000	23	-0.03200	-0.01600
24	-0.08700	-0.06700	25	0.00000	0.00000
26	-0.03500	-0.02300	27	0.00000	0.00000
28	0.00000	0.00000	29	-0.02400	-0.00900
30	-0.10600	-0.01900			

First, the state of the system with fixed UPFC parameters is estimated. The estimated system state and the power flow through line 6-4 are shown below.

#### State variables:

Bus No.	V	$\theta$ (Degree)	Bus No.	V	$\theta$ (Degree)
1	1.060000	0.000000	2	1.031817	-5.659963
3	1.007851	-8.391450	4	0.996201	-10.146324
5	0.990674	-14.968341	6	0.990340	-11.947724
7	0.981609	-13.742166	8	0.986904	-12.705754
9	1.033517	-15.428855	10	1.022804	-17.205907
11	1.077471	-15.509198	12	1.047093	-16.475904
13	1.077845	-16.476342	14	1.028016	-17.406134
15	1.020462	-17.474835	16	1.027567	-17.037637
17	1.018469	-17.393168	18	1.005346	-18.122725
19	1.000911	-18.305723	20	1.004929	-18.095308
21	1.008270	-17.689892	22	1.008590	-17.678446
23	1.003429	-17.894762	24	0.992111	-18.095032
25	0.978843	-17.724288	26	0.951628	-18.178112
27	0.984052	-17.197841	28	0.983836	-12.618487
29	0.951673	-18.624079	30	0.937921	-19.624272

#### Power flow in branch 6-4:

Bus No. (From)	Bus No. (To)	$P_{6-12} + jQ_{6-12}$
6	4	-0.7390 + j0.0437

Then, the UPFC model is incorporated into the state estimation formulation. In this case, the system is underspecified and, hence, an extra equation is needed. This equation will be provided by the power flow measurement which will now be set equal to the desired value of the flow through the device in branch 6-4, which in this example is set equal to -0.7 + j0.02, leaving all the other conditions the same.

The estimated state variables in this case are:

Bus No.	V	$\theta$ (Degree)	Bus No.	V	$\theta$ (Degree)
1	1.060000	0.000000	2	1.041838	-5.475726
3	1.016472	-7.995732	4	1.006776	-9.655479
5	1.011802	-14.350947	6	1.017156	-11.414607
7	1.007237	-13.143653	8	1.015091	-12.122612
9	1.070487	-14.395398	10	1.064048	-15.935696
11	1.115249	-14.395397	12	1.078960	-15.262148
13	1.109251	-15.262147	14	1.063893	-16.116744
15	1.058880	-16.191808	16	1.065156	-15.793472
17	1.059482	-16.101311	18	1.048793	-16.769330
19	1.045897	-16.928704	20	1.049670	-16.735522
21	1.051699	-16.364453	22	1.052165	-16.351227
23	1.047239	-16.554231	24	1.039953	-16.707064
25	1.031723	-16.253788	26	1.014302	-16.661620
27	1.035026	-15.723637	28	1.013930	-12.022441
29	1.015437	-16.925193	30	1.004106	-17.787005

The control variables and power of FACTS device are:

$\overset{\cdot}{V}_{B}$	$P_{\scriptscriptstyle B}$	$S_{\scriptscriptstyle B}$	$\stackrel{\cdot}{V}_{E}$	$P_{E}$	$S_E$
0.1392∠107.1456°	0.0127	0.0976	0.9924∠−11.5584°	-0.0127	0.1235

Note again that,  $P_B+P_E=0$ , and  $V_B\leq 1.0$ ,  $S_B\leq 1.0$ ,  $V_E\leq 1.0$ ,  $S_E\leq 1.0$ , where all the constraints are met.

Now the power flow in branch 6-4 is -0.7001 + j0.0200, which closely matches the desired set values.

This example illustrates that, by setting the control variables of UPFC to  $\dot{V}_B = 0.1392 \angle 107.1456^\circ$  and  $\dot{V}_E = 0.9924 \angle -11.5584^\circ$ , the power flow in branch 6-4 can be maintained at the desired amount.

#### 3.3 Conclusion

This part of the report presents an algorithm for state estimation of power systems embedded with FACTS devices. While only the Unified Power Flow Controller (UPFC) is used in the development, other types of controllers can easily be integrated into the developed prototype with minor effort. This program may have dual purposes. It can be used to estimate the controller parameters along with system state during normal operation. It can also be used to determine the required controller settings in order to maintain a desired power flow through a given line. Simulation results on IEEE 14-bus and 30-bus test systems are shown in order to illustrate the proposed usage of the developed program.

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# PART II: OPTIMAL METER PLACEMENT FOR MAINTAINING NETWORK OBSERVABILITY UNDER CONTINGENCIES

#### I. INTRODUCTION

#### 1.1 Introduction

Whether a new state estimator is put into service or an existing one is being upgraded, placing new meters for improving or maintaining reliability of the measurement system is of great concern. Determination of the best possible combination of meters for monitoring a given power system is referred to as the optimal meter placement problem. In choosing the types and locations of new measurements, there may be several different concerns, such as:

- Maintaining an observable network when one or more measurements are lost;
- Maintaining an observable network when one or more network branches are disconnected; and
- Minimizing the cost of new metering.

Our goal is to present a systematic procedure which can yield a measurement configuration that can withstand any one or more branch outages, or loss of one or more measurements, without losing network observability.

The paper [1] presented a topological method for single branch outages. The paper [2] proposed a unified approach, which generalized the meter placement problem formulation to simultaneously take into account both types of contingencies, namely loss of a branch or a measurement. The method is a numerical approach and can be implemented easily by modifying existing state estimation program. Furthermore, the total cost of adding measurements, as well as the number of additional measurements, are simultaneously minimized by an integer programming (IP) formulation. However, that method is only valid for loss of single measurements and single branch outages. In reality, a given power system may be subjected to contingencies which include loss of multiple measurements and/or multiple branch outages. Moreover, the unified method of [2] provides a way to introduce candidates for a single contingency, which requires only one

additional candidate measurement. If more than one candidate measurement is to be chosen for a contingency, then the IP problem needs to be reformulated so that proper IP constraints are used.

This part of the project addresses this need and improves the unified approach presented in [2] by extending it to the cases involving multiple measurement losses and multiple branch outages. The developed method is applied to several systems and results are presented.

#### 1.2 Problem Statement

The performance of a state estimator includes considerations of accuracy as well as reliability. A reliable state estimator should continue operating even under contingencies, such as branch outages or temporary loss of measurements. On the other hand, budgetary constraints prohibit expansion of measurement systems for the sake of redundancy. Hence, we should look at an optimization problem where the number of meters should be kept at a minimum while ensuring network observability for a predetermined set of contingencies.

One indictor of observability is the column rank of the measurement Jacobian, H, whose column rank is not affected by the operating point, but essentially depends on the measurement configuration. Therefore, it is sufficient to evaluate H at a flat start in order to study the effects of branch outages of loss of measurements on its rank.

Let the rows of Jacobian H be ordered so that the first  $m_e$  measurements are existing measurements. If the system is originally observable, the column rank of H will be full, i.e. equal to n the number of states. If H is found to be rank deficient, then proper pseudo-measurements should be added to make the rank of H full again. The choice of these additional measurements must be optimal so that the overall cost of adding these measurements is a minimum.

The solution of this problem is obtained in two stages.

- One stage is "candidate measurements identification", which is the selection of candidate measurement sets, each of which will make the system observable under a given contingency (loss of measurements and/or branch outages).

- The other stage is "optimal meter placement", which is the choice of the optimal combination out of the selected candidate measurement sets in order to ensure the entire system observability under any one of the contingencies.

#### II. PROPOSED ALGORITHM

#### 2.1 H matrix

H Matrix is the sub-matrix representing the gradient of the real power measurements with respect to all bus phase angles, in the decoupled model. Let the rows of the H measurement Jacobian be ordered such that the existing measurements are listed first as shown below:

$$H = \begin{bmatrix} H_{existing} \\ \Lambda \\ H_c \end{bmatrix} m_e \text{ existing measurements}$$

$$m_e \text{ candidate measurements}$$

where,  $m = m_e + m_c$  is the total number of measurements that are either already existing ( $m_e$  measurements) or likely to be installed ( $m_c$  measurements).

#### - Loss of Measurements

For the loss of one existing measurement k, we can set all entries of the *kth* row of the Jacobian H equal to zero. If a contingency includes several measurement losses, then we set all entries of corresponding rows equal to zero and have modified H matrix like:

$$H = \begin{bmatrix} H_e^{\text{mod}} \\ \vdots \\ H_c \end{bmatrix}$$

where  $H_e^{\text{mod}}$  represents the first  $m_e$  rows of H with row k replaced by a null row and  $H_c$  represents the remaining  $m_c$  rows corresponding to the candidate measurements.

#### Loss of branches

It is known that network observability will be drastically affected by topology changes. Assuming that one contingency includes one or more branch outages, for each branch outage, say k-j branch is outaged, some related elements of Jacobian are modified like:

$$H_{ik}^{\text{mod}} = H_{ij}^{\text{mod}} = 0$$
, if measurement  $i$  is a line flow;

$$H_{ij}^{\text{mod}} = 0$$
,  $H_{ik}^{\text{mod}} = H_{ik} + H_{ij}$ , if measurements *i* is an injection at bus *k*.

$$H_{ik}^{\text{mod}} = 0$$
,  $H_{ij}^{\text{mod}} = H_{ij} + H_{ik}$ , if measurements  $i$  is an injection at bus  $j$ .

After modifying the related elements of Jacobian for all branch outages in that contingency, we have the measurement Jacobian modified as:

$$H = \begin{bmatrix} H_e^{\text{mod}} \\ -H_c \end{bmatrix}$$

#### 2.2 Candidate measurements identification

For each pre-determined contingency, we can obtain the modified Jacobian H matrix by the method mentioned above for loss of measurements and branches.

Triangular factorization of the modified H matrix with row pivoting within existing  $m_e$  measurements will yield the following factors:

$$H = \begin{bmatrix} L_e \\ \overline{M}_r \\ \overline{M}_c \end{bmatrix} [U_e] \tag{2.1}$$

where the sparse lower triangular matrix  $L_e$  and sparse rectangular matrix  $M_r$  are corresponding to the existing measurements, and sparse rectangular matrix  $M_c$  is corresponding the candidate measurements.  $U_e$  is sparse upper triangular matrices. In carrying out the factorization procedure, row pivoting is restricted to the existing  $m_e$ 

measurements. If the rank of the sparse lower triangular matrix  $L_e$  is full (i.e. n for n+1 bus system), then the system is observable. If not, we have to select candidate rows from  $M_c$  to make the matrix rank full. Those selected candidate rows are corresponding to candidate measurements, which can be chosen to make the given system observable.

If the triangular factorization for the modified H matrix corresponding to one contingency still can proceed to the nth row, which means that the rank of H matrix still is full after the contingency, we will say that the contingency does not affect the observability of the system so we do not need to search for any candidate measurements.

If the result of triangular factorization on the modified H matrix implies that the rank of the matrix is n-1, which means the contingency results in making the system unobservable, we can select candidates from the lower rectangular factor, which looks like the following:

The measurements  $j_1$ ,  $j_2$  ... having nonzero in the nth column of the lower rectangular factor in the  $M_c$  will be selected as candidates for that contingency.

More generally, if the factorization of the modified H matrix for one contingency shows the rank is n-k; we will have the lower rectangular factor, which looks like the following:

For this case, additional k measurements are needed, and we have to select candidates from  $M_c$  to increase the rank.

For a given matrix A, the following properties are known to be true.

1. If P is a nonsingular matrix and PA = L, then rank(A) = rank(L).

2. If 
$$A = \begin{bmatrix} A_1 & 0 \\ A_2 & A_3 \end{bmatrix}$$
 then,  $rank(A) = rank(A_1) + rank(A_3)$ .

Upon factorization of the H matrix, those rows containing nonzero elements will be marked as possible candidates and denoted by the subscript "c". Assuming that there are C of such rows, any combination of k rows among these C nonzero rows, will yield the following:

$$\begin{bmatrix} L_e & 0 \\ M_{cl} & M_{cr} \end{bmatrix} \tag{2.4}$$

where  $M_{cl}$  and  $M_{cr}$  have k rows. If  $rank(M_{cr}) = k$ , then based on the property 2 above, the overall rank of H will be full. Otherwise, this set of possible candidates will be discarded from consideration since they will fail to render the system observable.

If we have l nonzero rows in  $M_c$  ( $l \ge k$ ), then we will have  $C_l^k$  sets of possible candidates. By the rank analysis of the sub-matrix  $M_{cr}$ , we will know the number of candidates among  $C_l^k$  sets of possible candidates, which can be selected to make the system observable.

Admittedly, the approach described above has its drawbacks in terms of the CPU requirements, particularly if many additional candidate measurements are needed to make the system observable, since we have to search for all candidate measurement combinations. Clearly the fewer additional candidate measurements that are needed, the less complicated it is to find all sets of candidates. In practice, however, there are very few cases that need more than five or more candidate measurements combined to make the system observable after a contingency, so this drawback is not considered to be of much practical significance.

# 2.3 Optimal Meter Placement

From the candidate selection procedure above, candidate measurements for each contingency can be obtained. The objective of the optimal selection procedure is to minimize the overall cost of this measurement system upgrade while making sure that all contingencies are properly taken into account. Each candidate measurement will be assigned an installation cost.

In order to obtain the optimal meter placement for those pre-determined contingencies, an Integer Programming (IP) problem such as the one below is constructed:

to minimize 
$$C^T \cdot X$$
 (2.5)

where C is a cost vector, and X is a binary candidate measurement status vector like:

$$X(i) = \begin{cases} 1 & \text{if meas "i" is selected} \\ 0 & \text{otherwise} \end{cases}$$
 (2.6)

The constraints of this IP problem will be:

- For the case that only one additional candidate measurement is necessary for the contingency,

$$\sum_{i} x_{i} \ge 1$$
; (measurement "i" is the candidate for the contingency)

- For the case that additional two candidate measurements are necessary for the contingency,

$$\sum_{i} x_{i_1} x_{i_2} \ge 1$$
; (measurements  $i_1$  and  $i_2$  are the candidates for contingency "i")

- For the case that additional *k* candidate measurements are necessary for the contingency,

$$\sum_{i} \prod_{k} x_{i_k} \ge 1 \text{ (measurements } i_1 \dots i_k \text{ are the candidates for contingency "i")}$$

The constraints in the IP problem ensures that each contingency is assigned candidate measurements whereas the objective function penalizes with respect to both the total cost as well as the number of selected candidates.

Solution of the IP problem described above yields measurements as the optimal choice that will ensure network observability under any pre-determined contingency at minimum cost.

# 2.4 Algorithm

The following algorithm is proposed for selecting candidates and determining optimal meter placement based on the above analysis:

- **Step 1:** Form the measurements H matrix, which include not only the existing measurements but also the non-existing measurements as the candidates.
- **Step 2:** For a contingency, modify the measurements H matrix, then perform the triangular factorization with row pivoting and row exchange within existing measurement rows, and obtain the column rank of the matrix.
- **Step 3:** Check if the column rank of the modified *H* matrix is full. If yes, go to **Step 4**. If not, select the candidate measurements that can make the *H* matrix full.
- **Step 4:** Check if all the contingencies have been done. If not, go to **Step 2**. If yes, the IP problem is constructed based on all selected candidates.
- **Step 5:** Yield the optimal meter placement, which ensures the entire system will remain observable under any one of the contingencies.

## Step 6: Stop.

# III. NUMERICAL EXAMPLES

# 3.1 6-bus system

The simple 6-bus system example with its measurement configuration shown in Figure 2.1 is considered to illustrate the proposed algorithm. All the branch impedances are set equal to j1.

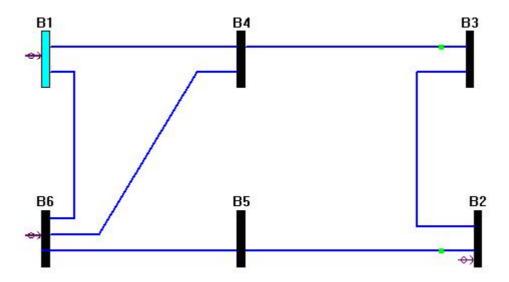


Figure 2.1 6-bus system example

All the measurements shown in the above Figure 2.1 are considered as existing measurements, and all the injection measurements and flow measurements, which are not shown in Figure 2.1, are considered as candidate measurements.

Existing Measurements = [Injections: 1, 2, 6; Flows: 2-5, 3-4].

Candidate Measurements = [Injections: 3, 4, 5; Flows: 1-4, 1-6, 2-3, 4-6, 5-6].

The chosen installation cost vector  $C^T$  corresponding to the candidate measurements is:

In this system we suppose that the contingency list includes the following loss of each single existing measurement, outage of each single branch, and two other contingencies

Contingency 1: branch 4-6 outage and loss of injection measurements at buses 1 and 6; and

Contingency 2: branch 2-3 outage and loss of injection measurement at bus 2.

The optimal meter placement algorithm should provide a set of additional candidate measurements which will ensure network observability after any of contingencies in the list above.

First we consider the optimal meter placement only for loss of single measurements and single branch outages, as stated in [2], not consider the other two contingencies.

For each contingency (either loss of single measurement or single branch outage), at most one additional candidate measurement is needed to make the system observable. By the method introduced in PART II, the candidate measurements, which are expressed as IP problem constraints, can be obtained for each existing measurement loss and each branch outage:

*Inj.* 1 Loss: 
$$x_2 + x_3 + x_4 + x_5 + x_7 + x_8 \ge 1$$

*Inj.*2 Loss: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7 + x_8 \ge 1$$

*Inj*.6 Loss: 
$$x_2 + x_3 + x_4 + x_5 + x_7 + x_8 \ge 1$$

Flow2 – 5 Loss: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7 + x_8 \ge 1$$

Flow3 – 4 Loss: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_8 \ge 1$$

Branch 2 - 3 Outage: 
$$x_2 + x_3 + x_4 + x_5 + x_7 + x_8 \ge 1$$

Branch 2 - 5 Outage: 
$$x_2 + x_3 + x_4 + x_5 + x_7 + x_8 \ge 1$$

Branch 3 - 4 Outage: 
$$x_2 + x_3 + x_4 + x_5 + x_7 + x_8 \ge 1$$

The outages of single branches 1-4, 1-6, 4-6 and 5-6 will not affect the network observability so that no IP constraint will correspond to them. The solution of the integer-programming problem yields the injection measurement at bus-4 as the optimal choice that will ensure network observability under any single branch outage or loss of single measurement at minimum cost 0.2. This result is same as the result from the method in [2].

Second, we consider the other two contingencies which include loss of several measurements and outage of several branches besides the contingencies of loss of single measurement and single branch outage. Besides the candidate measurements for the loss of single measurements and single branches, which are stated above, we also can obtain the candidate measurement sets for these two contingencies, which also are expressed as IP constraints:

Contingency 1: 
$$x_2 * x_3 + x_2 * x_5 + x_2 * x_8 + x_3 * x_4 + x_3 * x_5 + x_4 * x_5 + x_4 * x_8 + x_5 * x_8 \ge 1$$

Contingency 
$$2: x_2 + x_3 + x_4 + x_5 + x_7 + x_8 \ge 1$$

Obviously for Contingency 1, there are two additional candidate measurements needed to make the system observable. After considering these two contingencies, the IP solver shows that the optimal measurement set for this system is the injection measurements at buses 4 and 5 with the minimum installation cost 0.6. Hence, inclusion of these two additional measurements will maintain system observability during any single line outage or loss of any single measurement and these two contingencies in the 6-bus system.

# **3.2 14-bus system**

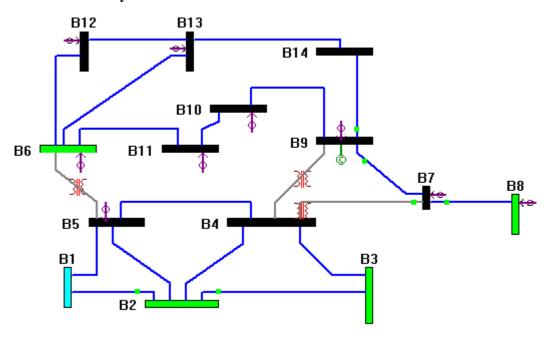


Figure 2.2 IEEE-14 system with measurements set

The IEEE-14 bus system with its measurement configuration shown in Figure 2.2 is also used to demonstrate the proposed method. All the measurements shown in the above Figure 2.2 are considered as existing measurements, and all the injection measurements and flow measurements, which are not shown in Figure 2.2, are considered as candidate measurements.

Existing Measurements = [Injections: 12, 13, 6, 11, 7, 8, 5, 9, 10; Flows: 9-14, 7-9, 4-7, 7-8, 1-2, 2-3].

Candidate Measurements = [Flows: 1-5, 2-4, 2-5, 3-4, 4-5, 4-9, 5-6, 6-11, 6-12, 6-13, 9-10, 10-11, 12-13, 13-14; Injections: 1, 2, 3, 4, 14].

The chosen installation cost vector  $C^T$  corresponding to the candidate measurements is:

$$[0.2, 1, 1, 1, 1, 1, 0.5, 0.5, 1, 0.4, 1, 0.6, 1, 0.5, 1, 1, 0.3, 0.6, 0.9]$$

First, we consider the optimal meter placement for loss of single measurements. As a result, the contingency list consists of loss of each existing measurement. For each contingency, at most one additional candidate measurement is needed to make the system observable. By the

method introduced in PART II, the candidate measurements, which are expressed as IP problem constraints, can be obtained for each existing measurement loss:

$$Inj.12: x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_9 + x_{10} + x_{13} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} \ge 1$$

$$Inj.13: x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_9 + x_{10} + x_{13} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} \ge 1$$

$$Inj.6: x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_{15} + x_{16} + x_{17} + x_{18} \ge 1$$

*Inj.*11: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_8 + x_9 + x_{10} + x_{13} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} \ge 1$$

$$Inj.5: x_1 + x_2 + x_3 + x_4 + x_{15} + x_{16} + x_{17} + x_{18} \ge 1$$

Inj.9: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_8 + x_9 + x_{10} + x_{11} + x_{12} + x_{13} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} \ge 1$$

Inj.10: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_8 + x_9 + x_{10} + x_{12} + x_{13} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} \ge 1$$

Flow 9 – 14: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_8 + x_9 + x_{10} + x_{11} + x_{12} + x_{13} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} \ge 1$$

Flow 
$$1 - 2: x_1 + x_2 + x_3 + x_4 + x_{15} + x_{16} + x_{17} + x_{18} \ge 1$$

Flow 2 - 3: 
$$x_4 + x_{16} + x_{17} + x_{18} \ge 1$$

Finally, solution of the integer-programming problem yields the injection measurement at bus-3 as the optimal choice that will ensure network observability under loss of any single measurement at minimum cost 0.3. However, since we exclude the redundant existing measurements in the candidate measurements, we decrease the complexity of the IP problem, which is important for the IP solver.

Second, we consider the contingencies including loss of several measurements and outage of single or several branches.

Contingency 1: loss of flow measurements in branch 1-2 and branch 2-3;

Contingency 2: loss of the injection measurement at bus 9, and loss of flow measurements in branch 9-14 and branch 9-7;

Contingency 3: loss of injection measurement at bus 7, and loss of flow measurements in branch 7-4 and branch 7-8;

Contingency 4: branch 10-11 outage; and

Contingency 5: branch 9-10 outage.

Besides the candidate measurements for the loss of single measurements, we also can obtain the candidate measurement sets for these five pre-determined contingencies, which also are expressed as IP constraints:

Contingecy 1: 
$$x_2 \times x_4 + x_2 \times x_{16} + x_2 \times x_{17} + x_2 \times x_{18} + x_3 \times x_4 + x_3 \times x_{16} + \Lambda \ge 1$$

Contingecy 2: 
$$x_{11} \times x_1 + x_{11} \times x_2 + x_{11} \times x_3 + x_{11} \times x_4 + x_{11} \times x_5 + x_{11} \times x_7 + \Lambda \ge 1$$

Contingency 3: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_8 + \Lambda \ge 1$$

Contingency 
$$4: x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_9 + x_{10} + x_{13} \Lambda \ge 1$$

Contingency 
$$5: x_1 + x_2 + x_3 + x_4 + x_5 + x_7 + x_9 + x_{10} + x_{13} \Lambda \ge 1$$

In each contingency, for space limitation, not all sets of candidate measurements are listed above. After considering these five pre-determined contingencies, the IP solver shows that the optimal measurement set for this system is to include the injection measurement at bus 3 and the flow measurement in branch 1-5. Hence, inclusion of these additional measurements will maintain the system observable during loss of any single measurement and these five pre-determined contingencies in the IEEE-14 bus system.

# 3.3 30-bus system

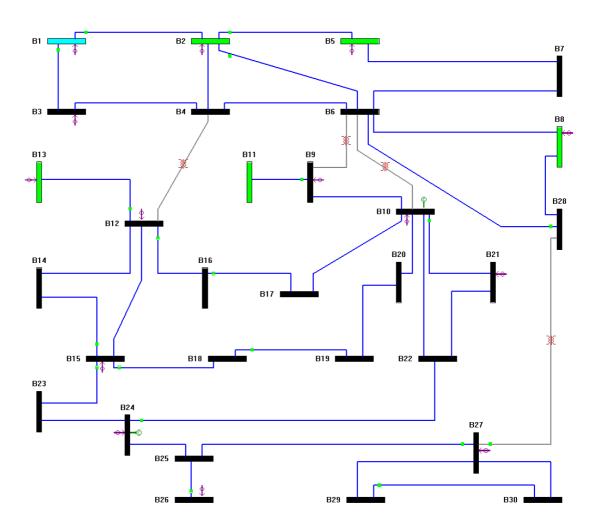


Figure 2.3 IEEE-30 system with a measurements set

Existing Measurements = [Injections: 1, 2, 3, 5, 8, 9, 10, 12, 13, 15, 21, 24, 26, 27; Flows: 1-2, 1-3, 2-5, 2-6, 9-11, 12-13, 12-16, 14-15, 16-17, 15-18, 18-19, 10-21, 15-23, 22-24, 25-26, 25-27, 28-27, 29-30, 6-28].

Candidate Measurements = [Injections: 4, 6, 7, 11, 14, 16, 17, 18, 19, 20, 22, 23, 25, 28, 29, 30; Flows: 2-4, 3-4, 4-6, 5-7, 6-7, 6-8, 6-9, 6-10, 9-10, 4-12, 12-14, 12-15, 19-20, 10-17, 10-20, 10-22, 21-22, 23-24, 24-25, 27-29, 27-30, 8-28].

The chosen installation cost vector  $C^T$  corresponding to the candidate measurements is:

[0.4, 0.4, 0.6, 0.8, 0.8, 0.4, 0.4, 0.4, 0.6, 1, 2, 1, 0.6, 0.6, 0.6, 0.6, 0.2, 0.2, 2, 0.2, 0.2, 2, 0.4, 1, 0.4, 1, 0.4, 0.4, 1, 0.8, 0.8, 0.6, 2, 0.4, 0.4, 0.2, 1, 0.2]

Similar to the previous two example systems, we consider loss of any single measurement at first. The corresponding IP constraints to loss of any single measurement are listed as follows:

*Inj*.5 Loss: 
$$x_2 + x_3 + x_{20} + x_{21} \ge 1$$

*Inj*.8 Loss: 
$$x_2 + x_{14} + x_{22} + x_{38} \ge 1$$

*Inj.*9 Loss: 
$$x_2 + x_9 + x_{10} + x_{23} + x_{25} + x_{29} + x_{31} \ge 1$$

*Inj*.10 Loss: 
$$x_9 + x_{10} + x_{29} + x_{31} \ge 1$$

Inj.12 Loss: 
$$x_1 + x_2 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{23} + x_{24} + x_{25} + x_{26} + x_{29} + x_{30} + x_{31} + x_{34} + x_{35} \ge 1$$

*Inj.*15 Loss: 
$$x_1 + x_2 + x_5 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{23} + x_{24} + x_{25} + x_{26} + x_{27} + x_{28} + x_{29} + x_{30} + x_{31} + x_{34} + x_{35} \ge 1$$

*Inj.*21 Loss: 
$$x_2 + x_7 + x_9 + x_{10} + x_{11} + x_{23} + x_{24} + x_{25} + x_{29} + x_{30} + x_{31} + x_{32} + x_{33} \ge 1$$

*Inj*.24 Loss: 
$$x_2 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{23} + x_{24} + x_{25} + x_{29} + x_{30} + x_{31} + x_{34} + x_{35} \ge 1$$

*Inj*.27 Loss: 
$$x_{15} + x_{16} + x_{36} + x_{37} \ge 1$$

Flow 
$$9-11: x_2 + x_4 + x_9 + x_{10} + x_{23} + x_{25} + x_{29} + x_{31} \ge 1$$

Flow 12-16: 
$$x_1 + x_2 + x_6 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{13} + x_{23} + x_{24} + x_{25} + x_{26} + x_{29} + x_{30} + x_{31} + x_{34} + x_{35} \ge 1$$

Flow 14-15: 
$$x_1 + x_2 + x_5 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{23} + x_{24} + x_{25} + x_{26} + x_{27} + x_{28} + x_{29} + x_{30} + x_{31} + x_{34} + x_{35} \ge 1$$

Flow 
$$16-17: x_6 + x_7 + x_9 + x_{10} + x_{29} + x_{30} + x_{31} \ge 1$$

Flow 15-18: 
$$x_1 + x_2 + x_5 + x_7 + x_8 + x_9 + x_{10} + x_{12} + x_{13} + x_{23} + x_{24} + x_{25} + x_{26} + x_{27} + x_{28} + x_{29} + x_{30} + x_{31} + x_{34} + x_{35} \ge 1$$

Flow 
$$18-19: x_8 + x_9 + x_{10} + x_{29} \ge 1$$

Flow 
$$10 - 21$$
:  $x_2 + x_7 + x_9 + x_{10} + x_{11} + x_{23} + x_{24} + x_{25} + x_{29} + x_{30} + x_{31} + x_{32} + x_{33} \ge 1$ 

Flow 22 – 24: 
$$x_2 + x_7 + x_9 + x_{10} + x_{11} + x_{12} + x_{13} + x_{23} + x_{25} + x_{24} + x_{29} + x_{30} + x_{31} + x_{34} + x_{35} \ge 1$$

Flow 25 – 27: 
$$x_2 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{15} + x_{16} + x_{23} + x_{24} + x_{25} + x_{29} + x_{30} + x_{31} + x_{33} + x_{34} + x_{35} + x_{36} + x_{37} \ge 1$$

Flow 28 – 27: 
$$x_2 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{14} + x_{15} + x_{16} + x_{23} + x_{24} + x_{25} + x_{29} + x_{30} + x_{31} + x_{33} + x_{34} + x_{35} + x_{36} + x_{37} \ge 1$$

Flow 
$$29-30: x_{15}+x_{16}+x_{36}+x_{37} \ge 1$$

Flow 6-28: 
$$x_2 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{14} + x_{12} + x_{23} + x_{24} + x_{25} + x_{29} + x_{30} + x_{31} + x_{33} + x_{34} + x_{35} + x_{38} \ge 1$$

Compared with the A matrix in [2], obviously some injection measurement losses are not listed here, such as loss of injection measurements at buses 1, 2, 3, 13, and 26. It is because loss of any of above five measurements will not affect the network observability and no extra measurement is needed.

Solving the IP problem as proposed, the optimal measurement set will be the injection measurements at buses 6and 19, and the flow measurement in branch 27-29 with minimum installation cost 1.2.

Next we include the other 5 contingencies into the contingency list besides loss of any single measurement.

Contingency 1: loss of injection measurement at bus 1, and flow measurements in branches 1-2 and 1-3;

Contingency 2: loss of injection measurement at bus 2, and flow measurements in branches 2-5 and 2-6; branches 1-2 and 2-4 are outaged;

Contingency 3: loss of injection measurement at bus 12, and flow measurements in branches 12-13 and 12-16;

Contingency 4: loss of injection measurement at bus 26, and flow measurement in branch 25-26; and

Contingency 5: loss of flow measurement in branch 29-30; branch 27-30 is outaged.

As a result, for the given contingencies list, besides the candidate measurements for the loss of single measurements, we also can obtain the candidate measurement sets for these five contingencies, which also are expressed as IP constraints:

Contingency 1: 
$$x_1 + x_2 + x_7 + x_9 + x_{10} + x_{12} + x_{13} + x_{17} + x_{18} + x_{19} + x_{23} + x_{24} + x_{25} + x_{29} + x_{30} + x_{31} + x_{34} + x_{15} \ge 1$$

Contingency 2: 
$$x_1 * x_3 * x_1 + x_2 * x_3 * x_7 + x_2 * x_3 * x_9 + x_2 * x_3 * x_{10} + x_2 * x_3 * x_{12} \Lambda \ge 1$$

Contingency 3: 
$$x_6 * x_7 + x_6 * x_9 + x_6 * x_{10} + x_6 * x_{29} + x_6 * x_{30} + \Lambda \ge 1$$

Contingency  $4: x_{13} \ge 1$ 

Contingency  $3: x_{15} + x_{16} \ge 1$ 

The IP solver shows that the optimal measurement set for this system is to include the injection measurements at buses 6, 19, 25, and 29, and the flow measurement in branch 5-7. Hence, inclusion of these additional measurements will maintain the system observable during loss of any single measurement and those five given contingencies in the IEEE-30 bus system.

# 3.4 57-bus system

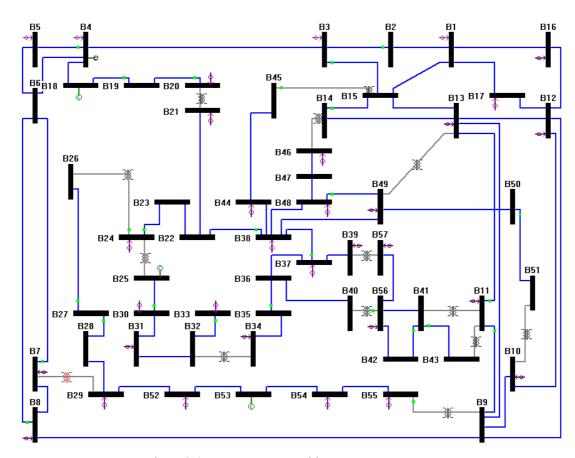


Figure 2.4 IEEE-57 system with a measurements set

Existing Measurements = [Injections: 1, 3, 4, 5, 7, 8, 10, 11, 12, 13, 16, 17, 20, 21, 24, 29, 30, 31, 33, 34, 37, 38, 39, 44, 46, 48, 49, 52, 54, 55, 56, 57; Flows: 2-3, 4-5, 6-7, 6-8, 9-11, 3-15, 18-19, 21-20, 24-26, 25-30, 22-38, 41-43, 15-45, 48-49, 50-51, 11-13, 14-15, 23-24, 26-27, 27-28, 32-33, 35-36, 37-38, 42-41, 40-56, 55-9].

Candidate Measurements = [Injections: 2, 9, 14, 15, 18, 19, 22, 23, 25, 26, 27, 28, 32, 35, 36, 37, 40, 41, 42, 43, 45, 47, 50, 51, 53; Flows: 1-2, 3-4, 4-6, 8-9, 9-10, 9-12, 9-13, 13-14, 13-15, 1-15, 1-16, 1-17, 4-18, 5-6, 7-8, 10-12, 12-13, 12-16, 12-17, 19-20, 21-22, 22-23, 24-25, 28-29, 7-29, 30-31, 31-32, 32-34, 34-35, 36-37, 37-39, 36-40, 11-41, 38-44, 14-46, 46-47, 47-48, 49-50, 10-51, 13-49, 29-52, 52-53, 53-54, 54-55, 11-43, 44-45, 41-56, 42-56, 39-57, 56-57, 38-49, 38-48].

The chosen installation cost vector  $C^T$  corresponding to the candidate measurements is set equal to 0.1.

First, we consider the loss of any single measurement. After obtaining all the IP constraints corresponding to the loss of any single measurement, the optimal measurement set will be the injection measurements at buses 14 and 32, with minimum installation cost of 0.2.

The corresponding IP constraints to loss of any single measurement are listed as follows:

*Inj.*29 Loss: 
$$x_8 + x_9 + x_{13} + x_{14} + x_{15} + x_{47} + x_{49} + x_{53} + x_{54} \ge 1$$

Inj.7 Loss: 
$$x_8 + x_9 + x_{13} + x_{14} + x_{15} + x_{25} + x_{47} + x_{49} + x_{50} + x_{53} + x_{54} + x_{66} + x_{67} \ge 1$$

*Inj*.24 Loss: 
$$x_{10} + x_{14} + x_{15} + x_{48} + x_{53} + x_{54} \ge 1$$

$$Inj.30 Loss: x_{14} + x_{15} + x_{51} + x_{52} + x_{53} + x_{54} \ge 1$$

*Inj*.31 Loss: 
$$x_{14} + x_{15} + x_{52} + x_{53} + x_{54} \ge 1$$

*Inj*.34 Loss: 
$$x_{14} + x_{15} + x_{53} + x_{54} \ge 1$$

*Inj*.29 Loss: 
$$x_8 + x_9 + x_{13} + x_{14} + x_{15} + x_{47} + x_{49} + x_{53} + x_{54} \ge 1$$

*Inj*.37 Loss: 
$$x_{14} + x_{15} + x_{16} + x_{17} + x_{53} + x_{54} + x_{55} + x_{57} \ge 1$$

*Inj*.39 Loss: 
$$x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{53} + x_{54} + x_{55} + x_{56} + x_{57} + x_{72} + x_{73} + x_{74} + x_{75} \ge 1$$

$$Inj.46 \text{ Loss}: x_4 + x_{22} + x_{60} + x_{61} \ge 1$$

*Inj*.48 Loss: 
$$x_4 + x_{22} + x_{60} + x_{61} + x_{62} \ge 1$$

Inj.52 Loss: 
$$x_8 + x_9 + x_{13} + x_{14} + x_{15} + x_{25} + x_{47} + x_{49} + x_{53} + x_{54} + x_{66} + x_{67} \ge 1$$

*Inj*.54 Loss: 
$$x_8 + x_9 + x_{13} + x_{14} + x_{15} + x_{25} + x_{47} + x_{49} + x_{53} + x_{54} + x_{66} + x_{67} + x_{68} \ge 1$$

Inj.55 Loss: 
$$x_8 + x_9 + x_{13} + x_{14} + x_{15} + x_{25} + x_{47} + x_{49} + x_{53} + x_{54} + x_{66} + x_{67} + x_{68} + x_{69} \ge 1$$

Inj.56 Loss: 
$$x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{53} + x_{54} + x_{55} + x_{56} + x_{57} + x_{72} + x_{73} + x_{74} + x_{75} \ge 1$$

Flow 2-3:
$$x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{53} + x_{54} + x_{55} + x_{56} + x_{57} + x_{72} + x_{73} + x_{74} + x_{75} \ge 1$$

Flow 24 – 26: 
$$x_8 + x_9 + x_{10} + x_{11} + x_{14} + x_{15} + x_{47} + x_{48} + x_{53} + x_{54} \ge 1$$

Flow 
$$25 - 30$$
:  $x_{10} + x_{14} + x_{15} + x_{51} + x_{52} + x_{53} + x_{54} \ge 1$ 

Flow 
$$41 - 43: x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{20} + x_{53} + x_{54} + x_{55} + x_{56} + x_{57} + x_{58} + x_{70} + x_{72} + x_{73} + x_{74} + x_{75} \ge 1$$

Flow 23 – 24: 
$$x_8 + x_9 + x_{10} + x_{14} + x_{15} + x_{47} + x_{48} + x_{53} + x_{54} \ge 1$$

Flow 
$$26 - 27: x_8 + x_9 + x_{11} + x_{12} + x_{14} + x_{15} + x_{47} + x_{53} + x_{54} \ge 1$$

Flow 27 – 28: 
$$x_8 + x_9 + x_{12} + x_{13} + x_{14} + x_{15} + x_{47} + x_{53} + x_{54} \ge 1$$

Flow 
$$35 - 36$$
:  $x_{14} + x_{15} + x_{16} + x_{53} + x_{54} \ge 1$ 

Flow 
$$42 - 41: x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{53}$$
  
  $+ x_{54} + x_{55} + x_{56} + x_{57} + x_{72} + x_{73} + x_{74} + x_{75} \ge 1$ 

Flow 
$$40 - 56$$
:  $x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{53} + x_{54} + x_{55} + x_{56} + x_{57} + x_{72} + x_{73} + x_{74} + x_{75} \ge 1$ 

Flow 
$$55-9: x_3 + x_8 + x_9 + x_{13} + x_{14} + x_{15} + x_{25}$$
  
  $+ x_{47} + x_{49} + x_{53} + x_{54} + x_{66} + x_{67} + x_{68} + x_{69} \ge 1$ 

Next, we include the other 5 contingencies into the contingency list besides the loss of any single measurement and outage of any single branch.

Contingency 1: loss of injection measurements at bus 4, and flow measurements in branches 4-5;

Contingency 2: loss of injection measurements at bus 24, and flow measurements in branches 23-24 and 24-26;

Contingency 3: loss of injection measurement at bus 48, and flow measurements in branches 48-49; branch 38-48 is outage;

Contingency 4: loss of injection measurement at bus 37, and flow measurement in branch 37-38; branch 36-37 is outage; and

Contingency 5: loss of injection measurement at bus 3, loss of flow measurement in branches 2-3, 3-15; branch 3-4 is outage.

As a result, for the given contingency list, besides the candidate measurements for the loss of single measurements and single branches, we also can obtain the candidate measurement sets for these five contingencies, which are expressed as the following IP constraints:

Contingency 1: 
$$x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_8 + x_9 + x_{14} + x_{15} + x_{16} + \Lambda \ge 1$$

Contingency 2: 
$$x_8 * x_9 * x_{10} + x_8 * x_9 * x_{14} + x_8 * x_9 * x_{15} + x_8 * x_9 * x_{48} + \Lambda \ge 1$$

Contingency 3: 
$$x_4 + x_{22} + x_{60} + x_{61} + x_{62} \ge 1$$

Contingency 4: 
$$x_{14} + x_{15} + + x_{16} + + x_{17} + x_{53} + x_{54} + x_{57} \ge 1$$

Contingency 5: 
$$x_1 * x_2 + x_1 * x_4 + x_1 * x_5 + x_1 * x_{21} + x_1 * x_{22} + \Lambda \ge 1$$

The IP solver shows that the optimal measurement set for this system is to include the injection measurements at buses 2, 22, and 23, and the flow measurements in branches 34-35 and 46-47. Hence, inclusion of these additional measurements will maintain the system

observable during any single line outage or loss of any single measurement and those five contingencies considered for the IEEE-57 bus system.

## 3.5 Conclusions

This part of the report presents several improvements to the unified measurement placement method by considering the loss of multiple measurements and/or multiple branch outages. Based on the modified measurement Jacobian H matrix for each contingency, a general candidate measurements selection method is introduced so that all candidates can be selected for loss of either single measurement and single branch or multiple measurements and multiple branches. Furthermore, the integer programming problem is extended to those cases where two or more candidates should be considered for placement due to a multiple contingency. Numerical examples verify the effectiveness of the proposed method for meter placement.

# REFERENCES

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# PART III: DESIGN OF DATA EXCHANGE ON DISTRIBUTED MULTI-UTILITY OPERATIONS

# I. INTRODUCTION

State estimation is essential for monitoring and control of a power system. In the historical regulated environment, the power system was owned and operated by local utilities using their own control area with a large amount of local generation to meet operational requirements. These utilities had the responsibility for and the ownership of the instrumentation in their local region to meet their needs for monitoring and control. There was little need to exchange extensive amounts of data with other organizations.

In recent years, those utilities have been releasing operational control of their transmission grids to form ISOs/RTOs while maintaining their own state estimators over their own areas [1]. In addition, a recent trend for these ISOs/RTOs is to further cooperate and facilitate a power market on as a Mega-RTO for better market efficiency [2]. The grid size of a Mega-RTO becomes extremely large, as concluded recently by the Federal Energy Regulatory Commission (FERC) that only four Mega-RTOs should cover the entire nation besides Texas [2].

many new problems ing achieving reliable state estimation arise under such an operating environment. First, state estimation over the whole grid of a Mega-RTO becomes very challenging because of its size. One possible scheme is to implement a new estimator over the whole grid, named as one state estimation scheme (OSE), which has many disadvantages in the aspects of investment and computation performance [3]. Recently, we developed a new concurrent non-recursive textured algorithm as an alternative [3], where the currently existing state estimators are fully utilized without using a new estimator. Such a distributed state estimation (DSE) algorithm evolves from the original well-developed textured algorithm in [4] with further distributed computations. The scheme also overcomes the disadvantages of OSE, and the additional cost in DSE is only some extra communication for some instrumentation or estimated data exchanges. In this part, the new issue is how to exchange instrumentation or estimated data with neighboring entities in a power market. This leads to three notes.

- 1) Data exchange design is critical to the newly developed textured distributed state estimation algorithm [3], which will be discussed in detail in the next part of the report.
- 2) Selected data exchange improves the quality of estimators in individual entities on both estimation reliability and estimation accuracy. In this report 'estimation reliability' refers to bad data detection and identification capability and probability to maintain observability under measurement loss.
- 3) After the introduction of data exchange, the traditional measurement placement methodology will be modified to fully utilize the benefit of data exchange.

Not all data exchanges are necessarily beneficial. In fact, some data exchange may harm the local estimators and thus the exchange has to be carefully designed. Experience alone cannot resolve the design issues. In particular, for big Mega-RTOs, no one has any experience yet.

Therefore, it is critical to develop a systematic approach to search for appropriate data exchange schemes. Since the computation complexity increases dramatically for large grids, data exchange design problem become very challenging.

Instrumentation/estimation data exchange issues in power market are discussed in [5]. Further studies are given in [6], where a new concept of Bus Redundancy Descriptor (BRD) is developed and utilized.

In this part, a knowledge-based system is proposed to efficiently search for beneficial data exchange scheme, and the additional new features include the following:

- 1) Based on BRD in [6], a new concept of Bus Credibility Index (BCI) is proposed, where the probability of good measurements is taken into account. Both BRD and BCI form the basis of the knowledge and BCI is a probability measure that quantifies the estimation reliability.
- 2) The improvement of estimation accuracy is discussed.
- 3) The economic factor on the implementation of data exchange is considered. Activities used to improve the quality of state estimation, including data exchange among member companies, are market-based and the economic cost must be taken into account.

4) The impact of the data exchange on traditional measurement placement methodology is discussed.

This part of the report is organized as follows. The concept of Bus Credibility Index (BCI) is discussed in Section II. The knowledge base of the expert system is described in Section III. Furthermore, in Section IV, the reasoning machine with the corresponding principles based on BCI is discussed. Numerical tests are studied in Section V. In the last section, a conclusion is drawn.

# II. BUS CREDIBILITY INDEX (BCI)

A sample system S in Fig.1 is used in this section to explain our newly developed concept.

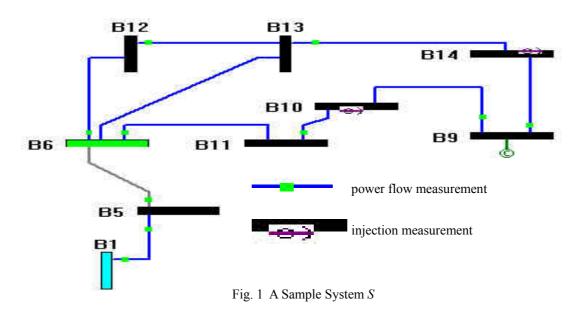
# 2.1 Basic analysis of state estimation

SE problem is based on the model [7]:

$$z = h(x) + e$$

where

z represents measurements,



e is the measurement noise vector,

x is the state vector composed of the phase angles and the magnitudes of the voltages on network buses, and

 $h(\bullet)$  stands for the nonlinear measurement functions.

WLS algorithm has been used to solve the SE problem in many commercial software packages for electric power system, which is based on a nonlinear iteration method. At each iteration i, the following equations is solved:

$$\Delta x_i = (H^T R^{-1} H)^{-1} H^T R^{-1} \Delta z_i = G^{-1} H^T R^{-1} \Delta z_i$$

where

R is the measurement covariance matrix,

H is the Jacobian matrix  $\partial h/\partial x$ , and

 $G = H^T R^{-1} H$  is the gain matrix.

# 2.2 Critical p-tuples

Critical p-tuples is first proposed in [8,9], and it is defined as a set of p measurements with respect to a specific system, where the removals of all the p measurements in the set will make the originally observable system unobservable. In addition, removals of any (p-1) measurements in the set will still keep the system observable.

The size of the critical p-tuples is defined as p. Critical p-tuples can be determined based on the analysis of symbolic Jacobian matrix H [10]. For example, the methodology in [11] can be used to determine the critical tuples. For the sample system S, 9-10, 10, and 12-13 are a critical 3-tuple, which is denoted as (9-10,10,12-13|S).

Note: "10" stands for the pair of active and reactive power injection measurement in bus 10, while "9-10" stands for the pair of the active and inactive power flow injection measurements from bus 9 to bus 10.

# 2.3 Weak Bus Sets of Critical p-tuples

The weak bus set of a critical p-tuples is determined as:

<u>Step1:</u> Remove all the p measurements in the critical p-tuples, and S becomes unobservable now.

*Step2*: Mark those lines with power flow measurements.

Step3: Select an unmarked line; if all the lines have been marked, stop and exit.

<u>Step4:</u> Add a pair of active and reactive flow measurements to this line for the time being and mark the line.

<u>Step5:</u> If S turns to be observable again, then the buses located on the two ends of this line belong to the Weak Bus Set of the critical p-tuples.

*Step6*: Remove the flow measurements just added in Step4, and go back to Step3.

For example, after the removal of (9-10, 10, 12-13|S), S becomes unobservable. If a pair of active and reactive flow measurements is added on line 6-13, the system becomes observable again. Therefore, buses 6 and 13 belong to the Weak Bus Set of (9-10, 10, 12-13|S). In fact, the Weak Bus Set of (9-10, 10, 12-13|S) is bus 6, 9, 10, 12 and 13, which is denoted as {6, 9, 10, 12, 13|(9-10,10,12-13)|S}.

## 2.4 Bus Redundancy Descriptor (BRD)

Every bus has its own Bus Redundancy Descriptor (BRD) with respect to a specific system. BRD of bus b is defined in [6] as a set of critical measurement p-tuples whose weak bus set includes bus b.

A bus is said to have a bus redundancy level g, if the smallest size of the critical tuples in its BRD is (g+1).

For example, it is determined in [6] that:

BRD(11,S)=
$$\{(6-11,6-12), (6-11,12-13), \dots\};$$

BRD(13,S)=
$$\{(6-11,6-12)(6-11,12-13)(6-12,12-13),(9-10,10,12-13),\ldots\}$$
.

Note: BRD(13,S)={(6-11,6-12) (6-11,12-13) (6-12,12-13), (9-10,10,12-13), ...} denotes BRD of bus13 with respect to S consists of three critical pairs (6-11,6-12), (6-11,12-13) and (6-12,12-13), a critical 3-triples (9-10,10,12-13), and other possible critical 4-tuples.

# 2.5 A new concept of Bus Credibility Index (BCI)

Bus Credibility Index of bus b is defined as the state estimation credibility probability on bus b with respect to a specified system. BCI can be determined as:

$$BCI(b, S) = 1 - P(C_1 \cup C_2 \cup \cdots \cup C_k)$$

$$=1-\sum_{i=1}^k \left((-1)^{i-1}\sum_{1\leq t 1 < t 2 < \cdots < t i \leq k} P(C_{t1} \cap C_{t2} \cap \cdots \cap C_{ti})\right)$$

$$=1-(\sum_{1\leq t}P(C_{t1})-\sum_{1\leq t}P(C_{t1}\cap C_{t2})$$

$$+\sum_{1\leq t \mid < t \leq < t \leq \leq k} P(C_{t1} \cap C_{t2} \cap C_{t3}) - \cdots + (-1)^{k-1} P(C_{1} \cap C_{2} \cap \cdots \cap C_{k}))$$

$$(1)$$

where

BCI(b,S) is the BCI of bus b with respect to system S;

BCD(b,S) consists of k critical p-tuples Ci, p=1,2,3,...;

 $P(C_i \cap C_j)$  stands for the failure probability when all measurements in Ci and Cj fail.

If the failure probabilities of measurements are independent from each other, then  $P(C_i \cap C_j)$  can be determined by:

$$P(C_i \cap C_j) = P(\{M_1, M_2, \dots, M_l\}) = P(M_1) \cdot P(M_2) \cdots P(M_l)$$
(2)

where

 $\{M1, M2, ..., MI\}$  are the measurement set which makes up  $(C_i \cap C_j)$ ,

P(MI) stands for the failure probability of MI.

Given the failure probability of every measurement, BCI(b,S) can be determined according to equations (1) and (2).

For example, suppose the failure probability is fixed to 0.01, BCI(b,S) is determined as Table 1:

Table 1 BCI of Buses With Respect to Sample System in Fig. 1

BCI(5,S)	BCI(11,S)	BCI(13,S)
0.9900	0.9998	0.9997

#### 2.6 Remarks

- The meaning of BCI depends on the definition of failure probability. If the failure probability of measurements stands for the probability of measurement availability, then BCI(b,S) stands for the probability to maintain observability on bus b with respect to system S since the removal of all measurements of a critical k-tuples will make S unobservable. If the failure probability of a measurement stands for the probability of bad data in this measurement, then BCI(b,S) reflects the probability to successfully identify bad data since bad data cannot be identified if all the measurements of a critical k-tuples are bad data. Therefore, BCI is a probability measure that quantifies the estimation reliability on bus b with respect to a specific system S.
- Remark 2: If BCI(b1,S1)>BCI(b2,S2), then bus b1 with respect to system S1 is said to be stronger than bus b2 with respect to system S2.

Note that data exchanges modify the original system S to S', and the incremental difference of BCI from (b,S) to (b,S') stands for the benefit of such a data exchange on bus b in the sense of estimation reliability.

• As pointed out in [6], a critical k-tuples not necessarily constitutes a connected measurement area, and the weak bus set of a critical tuples is also not limited to the buses linked directly to the measurements of the critical tuples.

The measurements in BRD(b,S) either connect directly with b or locates on a loop that includes b. For example, BRD(b5,S) consists of (5-6) and (1-5,5-1) which connect directly with b5, and

BRD(b13,S) consists of critical tuples such as (6-11,6-12), (6-11,12-13), (6-12,12-13) and (9-10,10,12-13), which are all located in the loop  $b6 \rightarrow b12 \rightarrow b13 \rightarrow b14 \rightarrow b9 \rightarrow b10 \rightarrow b11 \rightarrow b6$ .

- Given the condition that the failure probability of every measurement is very low (<0.01), then the failure probability of the critical k-tuples where k is large enough can be ignored in the computation of BCI. For example,  $BCI(b,S) \approx 1.0000$  if the redundancy level of b with respect to S is greater than 3, and only buses with redundancy level less than 4 are potential weak parts of the system, which we should focus on.
- With the full consideration of measurement failure probability, BCI(b,S) is a more accurate criterion to evaluate the estimation reliability compared with local or global bus redundancy level.

## III. KNOWLEDGE BASE

The knowledge base of the proposed expert system consists of the following parts.

## 1. Raw Facts

Raw facts refer to the data input directly by the user, such as:

- The configuration, parameters and ownership of current power system network and measurement system;
- 2) The failure probability and accuracy of measurements; and
- 3) The cost of instrumentation and estimated data exchange.

Importance of raw facts is rather clear. However, the knowledge is too primitive to be informative. Therefore, more refined information, such as the BCI information and the estimation accuracy information, must be extracted by an expert system based on the raw facts.

## 2. BCI Information

BCI(b, S) reflects the estimation reliability on bus b with respect to a specific system S, which is very useful in data exchange design.

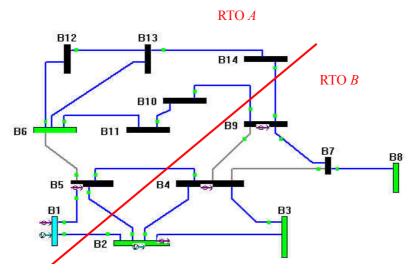


Fig. 2 Two RTOs merge into one Mega-RTO

## 3. Variance of SE errors

It is well known [12] that the variances of the SE errors stand for the accuracy of SE. Statistically, they represent the "squared distances" of the estimates from their true values. The smaller the variances are, the better the SE solution is typically.

The state estimation error variances are the diagonal elements of matrix  $C = G^{-1}$ .

Since the error variances are only slighted influenced by the operation point, the comparison of different data exchange scheme is executed on a uniform given operation point.

# IV. REASONING MACHINE

An IEEE-14 bus system as shown in Fig. 2 is used to illustrate how the reasoning machine works, where RTO-A and RTO-B will merge into one Mega-RTO. There are two existing local estimators for systems A and B, where neither overlapping areas nor data exchange is involved. The algorithm and principles are not limited to the selected examples; they are applicable to all systems.

We have explored ways in [3] to design a distributed state estimator from the existing estimators instead of building a totally new estimator for the whole system. In this part, the design of data exchange scheme is the focus. Data exchange is a prerequisite for the algorithm in [3]; when properly designed, it will be beneficial to local estimators.

A measurement system can be evaluated through different criteria, among which the most important criterion is estimation reliability and estimation accuracy. As discussed before, 'estimation reliability' refers to bad data detection and identification capability and probability to maintain observability under measurement loss, which is evaluated by BCI. Therefore, in the following algorithm, we focus on only BCI instead of estimation reliability.

The processes in the reasoning machine are given below.

**Step 1:** Determine the maximum possible benefit on BCI after data exchange by:

$$BCI(b_A, Whole) - BCI(b_A, A)$$
 and  $BCI(b_B, Whole) - BCI(b_B, B)$ 

where  $b_A$  are the boundary buses in A, such as b1,b5,b10,b14;

b<sub>B</sub> are the boundary buses in B, such as b2,b4,b9;

Whole stands for the whole system of Mega-RTO.

Only boundary buses are of concern because, in most cases, BCI of internal buses also improves when BCI of boundary buses improve, although the rate is much smaller.

<u>Step 2:</u> If the maximum possible benefit of a boundary bus is less than a pre-defined threshold, then this boundary bus will be ignored during the following searching process.

<u>Step 3:</u> For a given boundary bus  $b \in \{b_A \cup b_B\}$ , some rules are used to search for beneficial data exchange:

# Rule 1 for Instrumentation Data Exchange:

For boundary bus  $b_A$  in A, instrumentation data exchange should extend to boundary bus  $b_B$  in B given the condition  $BCI(b_B, Whole) > BCI(b_A, A)$ . For example, it is reasonable for b2 and b4 in B to extends to include b1 and b5 in A, while it does not follow the principle that b9 in B extends to include b10 or b14 in A.

## Rule 2 for Instrumentation Data Exchange:

The final configuration after data exchange should avoid forming a radial structure; instead, a loop is preferred. For example, branch b1-b5 and b5-b2 should also be included in B after data exchange to avoid radial branch b2-b1 and b4-b5. On the other hand, b9 in B extend only to b10 in A will form a new radial branch b9-b10, which violates this principle.

## Rule for Estimation Data Exchange:

**Step 1**: If BCI(b, A) > BCI(b, B) where b is in the common part of A and B, then estimation result exchange from A to B on this bus will improve BCI(b, B) to the magnitude of BCI(b, A).

Estimation accuracy information is not used here because BCI is more important than estimation accuracy in industry applications. Furthermore, in most cases, estimation accuracy improves when BCI improves.

**Step 2:** System A and B are modified accordingly based on the newly found data exchange from Step 1. BCI, estimation accuracy and the economic cost are evaluated on the 'new' system A and B to verify the benefit.

<u>Step 3:</u> If BCI on the given bus b of the post-data-exchange system are close enough to that in the whole system, then we can stop searching for new data exchange for bus b. Otherwise new data exchange can be searched further.

**Step 4:** Step 3 is repeated on all boundary buses of A and B.

Under power market environment, economic factors are especially important and are considered in the reasoning machine I the following ways.

1) The benefit of different data exchange schemes may differ greatly. The benefit may saturate after some data exchange, which implies no major benefit can be obtained for more data exchange.

- 2) The hardware/software cost on data exchange implementation should be minimized given the condition that the performance is satisfied. In other words, even if scheme D1 is slightly better than scheme D2 in performance, but it is still possible for industry to select D1 when D1 is much more economical than D2.
- 3) The price tag of a data reflects not only the installation cost but also its market value. It is possible for system A to attach a rather high price tag to a measurement that is especially useful to system B. The proposed expert system is critical for the companies to determine the market price based on the benefit of data exchange.
- 4) Since new measurements can be sold to other companies, the data exchange will have some impact on measurement placement decision. Accordingly, the proposed expert system is useful for both the design of the data exchange scheme and the new measurement placement decision.

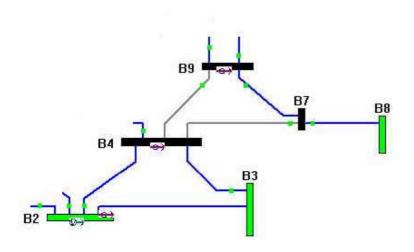


Fig.3 Original System of B before data exchange

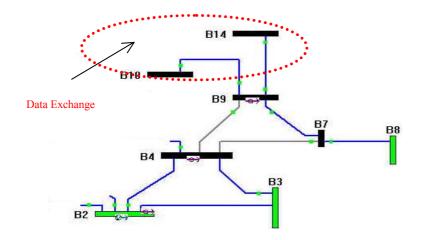


Fig.4 Modified System of B after data exchange

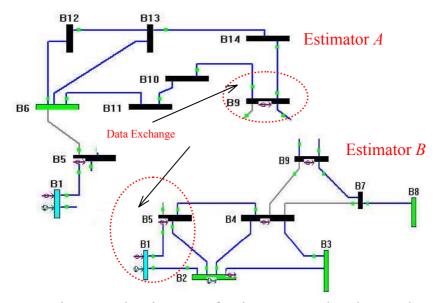


Fig.5 Local estimators after instrumentation data exchange

# V. NUMERICAL TESTS

The following cases demonstrate several points.

- 1. Not all data exchange is beneficial. In fact, some data exchange may harm the local estimators in both estimation reliability and estimation accuracy.
- 2. With a few data exchanges, both estimation reliability and estimation accuracy of local estimators can be improved to the level as high as that of the one estimator on whole system.
- 3. The data exchange has an impact on traditional new measurement placement approach.

Estimation reliability is evaluated via BCI.

# 5.1 Case 1: Harmful Data Exchange Scheme

RTO B with a data exchange scheme is given in Fig. 4 and the original system before data exchange is given in Fig. 3. As mentioned before, such a data exchange does not follow our principles. In fact this data exchange scheme is harmful for Company B, which is demonstrated in the following way.

The comparison between original B and modified B is given as follows (given the bad data probability of any measurement is 0.1, and the accuracy of any measurement is 0.01 p.u.):

Table 2 Average BCI On The Buses Of Company B

B in Fig. 3	B in Fig. 4	B in Fig. 5	Whole System
0.9647	0.9643	0.9662	0.9662

Table 3 Average Estimation Error On The Buses Of Company B

B in Fig. 3	B in Fig. 4	B in Fig. 5	Whole System
7.7314e-007	8.1738e-007	2.6471e-007	2.6326e-007

Table 4. Normalized Residues for Local Estimator B

Iteration	Estimator B in Fig. 3		Estimator B in Fig. 4	
No.	Meas.	Max. Residue	Meas.	Max. Residue
1st	9	164.72	9-4	89.41
2nd	9-7	108.05	7-4	56.78
3rd	No bad data detected		4	34.68
4th	N/A		No bad data detected	

Table 2 implies that the data exchange shown in Fig. 4 decreases B's BCI, which means such a data exchange scheme decreases estimation reliability. The following example demonstrate our conclusion.

Suppose that both measurements, 9 and 9-7, are bad data in which the sign of these measurements are reversed. When the measurement with largest normalized residue is removed as bad data in WLS algorithm for SE, the SE is executed again to find other possible bad data. Table 4 shows the result of such an iteration process. It is clear that before data exchange (Fig. 3) these two bad data are detected, identified, and removed correctly while after data exchange (Fig. 4) these bad data cannot be even detected at all.

The feature of this example is that even though the exchanged data are with no bad data, the estimation reliability on local area is still seriously harmed after data exchange.

Table 3 indicates that B's estimation error also increases after such a data exchange.

# 5.2 Case 2: Efficiency of Beneficial Data Exchange

Our expert system suggested an optimal data exchange scheme following our principles:

- Instrumentation data exchange: shown in Fig. 5.
- Estimation data exchange: Estimation result on bus 1 and 5 are exchanged from B to A. The detailed algorithm to utilize these estimated data is given in detail in [3], which will be discussed in the next part of the report.

Tables 2 and 3 compare the performances of distributed SEs and the whole system estimator. It is clear that:

- 1) B in Fig. 5 improves the BCI over the buses belonging to original system in Fig. 3. Furthermore, BCI for B shown in Fig. 5 is as good as the whole system estimation. It shows that little benefit on BCI could be further gained through more data exchange.
- 2) B in Fig. 5 has improved its estimation accuracy over the original system in Fig. 3. Furthermore, the accuracy difference between Fig. 5 and the whole system is rather small, which shows that little benefit on estimation accuracy could be further gained through more data exchange.
- 3) After data exchange, the local estimator achieves estimation reliability and estimation accuracy as high as the one estimator for the whole system.

# 5.3 Case 3: Impact on New Measurement Placement (1)

Suppose the probability of accidents in the SCADA on station b1 is extremely high. Obviously, such an accident would cause the voltage measurement on b1, power injection measurement on bus1, power flow measurements 1-2 and 1-5 to all be unusable for the state estimation. Accordingly, the system would become unobservable, which is unacceptable for RTO A.

From the traditional measurement placement viewpoint, in order to keep state estimation running smoothly, at least one new measurement has to be installed, such as voltage measurement on bus 5.

However, with data exchange, such a new measurement is not necessarily needed. When we follow the data exchange scheme suggested in Case 2, the state estimation in RTO A can be run normally even after the accident happened because the estimation result on b1 and b5 is exchanged from B to A.

# 5.4 Case 4: Impact on New Measurement Placement (2)

Suppose that RTO A wants to improve the estimation accuracy on b5. From a traditional measurement placement viewpoint, there are basically two alternatives: improve the accuracy from original 0.01 to 0.001 on the measurement 5-1 or 5-6. These two alternatives have basically the same effect to improve the estimation accuracy on b5.

On the other hand, if the accuracy of measurement 5-1 improves, the accuracy of RTO B also improves if measurement 5-1 is exchanged from A to B. Therefore, it makes sense for RTO B to share part of the cost with A to improve the accuracy of 5-1. Accordingly, it is better for A to invest on measurement 5-1 instead of on measurement 5-6.

# VI. CONCLUSION

In this part of the report, a knowledge-based system was proposed to search for beneficial data exchanges for distributed state estimations. The knowledge includes the information on Bus Credibility Index (BCI), which reflects the estimation reliability. The reasoning machine consists of a few principles, where economic factors are also considered. Numerical tests on IEEE-14 bus system demonstrate that properly selected data exchange improves the estimator quality of all entities on both estimation reliability and accuracy. In addition, data exchange has an impact on traditional measurement design. It was also shown that the benefit of data exchange schemes can be quite different. Properly selected data exchanges will enable the performance of the local distributed estimator to be as high as one estimator on the whole system in both estimation reliability and estimation accuracy. On the other hand, poorly designed data exchanges which do not follow our design rules may be harmful to local estimators.

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# PART IV: A CONCURRENT TEXTURED DISTRIBUTED STATE ESTIMATION ALGORITHM

#### I. INTRODUCTION

As mentioned in part 3, power companies are releasing their transmission grids to form ISOs/RTOs [1] while still maintaining their own local state estimators. In other words, companies run their own SE's and focus on the quality of SE in their own area. Therefore, there are multiple state estimators distributed with different owners in one ISO/RTO. Furthermore, a recent trend for these ISOs/RTOs is to further cooperate to run the power market on even a bigger grid, such as a Mega-RTO, for a better market efficiency [2]. The grid of an ISO/RTO could be large. The size of a Mega-RTO is even bigger, as concluded recently by Federal Energy Regulatory Commission (FERC), that only four Mega-RTOs should cover the entire nation [2]. The state estimation over the whole grid becomes very challenging just for its size.

One possible scheme is to implement a totally new estimator over the whole grid, and one state estimator (OSE) is executed over the whole system. However, the OSE approach has many disadvantages.

- 1) The investment in the new estimator could be enormous. The maintenance cost over such a huge area is also high.
- 2) The size of the system is extremely large, which raises the scalability issue. The system matrix becomes more ill-conditioned, and the computation speed and convergence performance becomes slower and poorer.
- 3). The existing local state estimators distributed in different entities are wasted.

Because of the disadvantages of OSE, a new concurrent, non-recursive textured algorithm is developed as an alternative to determine the state of the whole grid, where the currently existing state estimators are fully utilized without using a new estimator. This textured algorithm is a distributed state estimation (DSE) algorithm, which overcomes the disadvantages of OSE.

The concurrent textured algorithm has been well developed to deal with the optimization problem of power systems by our team led by Dr. Huang [3, 4, 5]. The basic idea of a textured algorithm is as follows [3]. First, the problem on a large system is decomposed into several smaller and more tractable sub-problems for concurrent computation by fixing some boundary variables. Then, by rotating the fixed variables, a recursive sequence of concurrent sub-problems are solved and the original high dimension problem is solved by divide-and-conquer. The term 'texture' is because there are overlapping areas between the neighboring sub-systems, which are just like texture. And the boundary variables are located on these overlapping areas.

The introduction of such a concurrent textured algorithm into the state estimation problem avoids the disadvantages of OSE. Furthermore, as compared with existing DSE algorithm [6,7,8], the performance of the new algorithm improves greatly with respect to bad data detection and identification ability, and to avoiding discrepancy on boundary buses.

The main flowchart and advantages of the new algorithm are discussed in Section II. The selection of a data exchange scheme, as the center issue of the textured decomposition method, is described in Section III. Furthermore, in Section IV, the sparse matrix technique and its application are discussed. The determination of the state over the whole system is given in Section V. Numerical tests are studied in Section VI. In the last section, Section VII, a conclusion is drawn.

## II. CONCURRENT TEXTURED DSE ALGORITHM

# 2.1 Existing DSE Algorithms and their Drawbacks

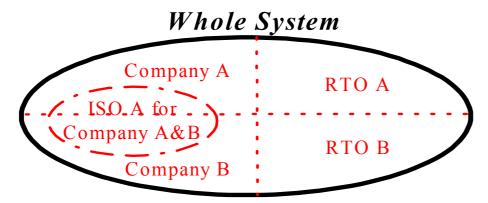


Fig. 1 Multiple Companies/ISOs/RTOs connected physically

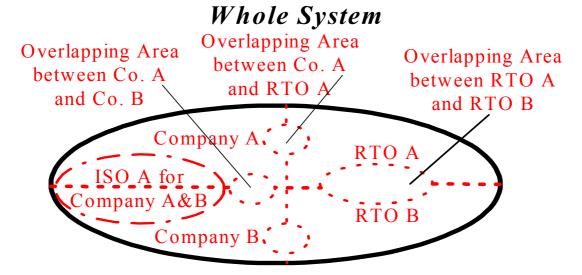


Fig. 2 Overlapping areas come into being after data exchange

Assume multiple entities such as companies, ISOs and RTOs, are connected physically and cooperate to run the whole system as Fig. 1. Accordingly, there are multiple existing estimators distributed in the sub-systems like Company A, Company B, ISO A, RTO A and RTO B. And every entity maintains and executes their local state estimation on their own areas. These entities are connected through tie lines near the boundary buses.

With the development of Information Technology (IT), DSE algorithms, especially those without central controlling node [6, 7], become more and more applicable.

The main drawback of the existing DSE algorithms [6,7,8] is that bad data detection and identification ability decreases greatly compared to OSE which is over the whole system, especially when bad data are close to the boundary of individual estimators. Moreover, the estimation accuracy on boundary buses are much lower than OSE, which decrease the accuracy in determination of the global reference bus and which make the whole result inconsistent.

# 2.2 Introduction of a New Algorithm

The objective of our new algorithm is to remove the drawback of existing DSE algorithm while preserve the beneficial characteristics. In the new algorithm, there are some overlapping areas in the neighboring estimators as shown in Fig. 2, where some information are shared.

Furthermore, the point here is to extend the sharing information; not only are the boundary buses shared formally in the estimation sub-problems, as in [6], but also instrumentation data (real time measurement information before execution of local estimator) and estimated data (estimation results after execution of local estimator) are exchanged among neighboring entities. Such a data exchange is introduced simultaneously between multiple entities, such as Company A and Company B, ISO A and Company B, Company B and ROT B, and so on. Accordingly, a textured network is formed.

#### 2.3 Main Algorithm

The new algorithm is described as follows:

- **Step1**: Select a set of real time instrumentation data to be exchanged between neighboring entities.
- Step2: Select a set of estimated data to be exchanged between neighboring entities.
- *Step3:* Taking the exchanged instrumentation data into account, the multiple local estimators distributed in different entities are executed simultaneously and asynchronously until they converge individually to the desired tolerance.
- **Step 4:** In view of the exchanged estimated data, modify the estimation result of local estimators accordingly and re-run bad data analysis.

• *Step5*: Based on the modified results of local estimators, finally determine the state of the whole system according to the different accuracy and reliability of estimators.

#### 2.4 Advantages of the New Algorithm

• Advantage 1: Bad data detection and identification ability in the new algorithm is higher than the existing DSE algorithm, especially when bad data appear close to the boundary of individual estimators. Such an improvement is because of the cooperation between estimated data exchange scheme and the textured network formed by instrumentation data exchange.

For example, in the existing DSE algorithm, if bad data appears in the boundary of one local estimator A, then it is hard to be detected in A. However, in a textured decomposition environment, the boundary buses in A are internal buses of another estimator (for example B) at the same time, where the bad data can be detected. And the corrected information on these buses will be exchanged from B to A via estimated data exchange, which will finally make A also capable to detect the bad data. This capability suits well for an industrial environment in which it is better to obtain SE results with good enough accuracy without bad data than the results with higher accuracy, but with possible undetected bad data.

- Advantage 2: The estimation accuracy on boundary buses is much higher than existing DSE and is comparable to OSE. Our approach decreases the discrepancy on the boundary buses and makes the whole result more consistent.
- Advantage 3: Many earlier methods of DSE assume a star-like function network [8] where the communications between the multiple remote processors and the central computer are critical during iteration processes. Such a hierarchical approach suffers from bottleneck and reliability issues because of the central controlling node. Our concurrent textured algorithm is asynchronous without a central controlling node. As a consequence, the new algorithm becomes very fast and practical.
- Advantage 4: Utilizing the instrumentation decoupling nature in SE, we removed the recursion process in our original optimization. At the same time, the performance of estimation is still

satisfied, which is verified in our numerical tests. As a consequence, the speed of our new algorithm gets even faster. This further advances our original textured algorithm.

- Advantage 5: The multiple local estimators can use different SE algorithms. Furthermore, the convergence tolerance can be different based on different quality of local measurement systems. Accordingly, our new algorithm becomes very flexible in which current existing estimators can be included easily.
- Advantage 6: The performance of bad data detection and estimation accuracy in individual existing estimators improves as well, which benefits individual companies/ISOs/RTOs. Accordingly, they are more willing to share the information for their own benefits.

#### III. DSE TEXTURED DECOMPOSITION METHOD

#### 3.1 Introduction

As discussed, we need to determine an instrumentation data and estimated data exchange scheme to be used in Step 1 and Step 2. As special cases, if all the information is exchanged and shared, the estimation becomes one estimator over the whole system, an OSE but not a DSE. On the other hand, if no measurement is exchanged, it becomes the existing DSE algorithm, which has the drawbacks described before. Therefore, a trade-off in the selection of data exchange is necessary to make the overlapping areas moderate, not too large nor too small. Then, an appropriate texture can be formed, which is a critical precondition for our new algorithm.

In addition, in the original textured decomposition method [3-5], the decomposition is based on the requirements of the algorithm. However, in the DSE problem, the range of individual estimators has been determined in advance from the actual industry ownership. And the hardware/software cost on data exchange implementation should be minimized, which implies schemes with smaller overlapping areas are preferred if all the other performance remains the same.

Not all the data exchange is beneficial. In fact, some data exchange may harm the local estimators and thus the exchange has to be carefully designed. Experience alone cannot resolve the design issues. In particular, for big mega-RTOs, no one has any experience.

Therefore, it is critical to develop a systematic approach to search for appropriate data exchange schemes, which can also help the design automation process.

# 3.2 A Systematic Textured Decomposition Method

Our effective data exchange scheme design method and the corresponding software have been proposed to determine the textured decomposition by us in [9], which is discussed in the previous part of the report. A simple description is given below.

The strength of bus b in estimator A is defined as the bad data detection and identification ability and estimation accuracy on bus b in this particular estimator A. A newly developed concept of Bus Redundancy Descriptor (BRD) is used to numerically evaluate the strength of every bus in different estimators. Details of the definition of BRD and determination of strength are given in [9].

Accordingly, two main rules are proposed by us [9] to search for the estimated data/instrumentation exchange, which is a critical part of textured decomposition.

After data exchange, the strength of buses improves greatly. And the ultimate objective is that the strength of every bus in the local estimators is almost as high as that in OSE. As for the buses in the overlapping areas of different local estimators, the objective is to ensure that the strength of these buses is high enough in at least one local estimator. The accomplishment of such an objective is critical to obtaining the advantages 1 and 2 of the new algorithm.

In addition, artificial intelligence (AI) is widely used to deal with problems described with uncertain terms like 'almost'. Therefore, the application of AI to the textured decomposition problem is quite natural.

# 3.3 Numerical Examples

Different distribution of local estimators will leads to different textured decomposition schemes.

For example, in an IEEE-14 bus system as shown in Fig. 3, RTO-A and RTO-B will merge into one Mega-RTO. There are already two local estimators A and B, distributed in RTO A and RTO B, with neither overlapping areas nor data exchange. In other words, no texture exists in the local estimators.

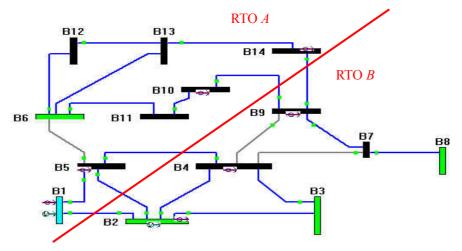


Fig. 3 Two RTOs merge into one Mega-RTO

A suggested textured decomposition is shown in Fig. 4.

# Instrumentation Data Exchange:

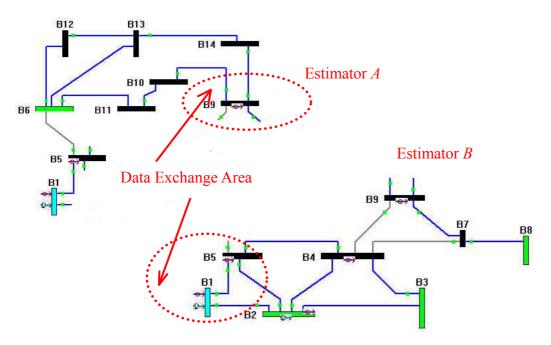


Fig. 4 Local estimators after raw data exchange

Estimator A expands to include bus 9. Furthermore, the instrumentation data on these buses, such as 9-10 (power flow measurements from bus 9 to bus 10), 9-14 and 9 (power injection measurement on bus 9), are also exchanged from B to A in a real time manner. And estimator A is executed in such an expanded sub-system.

Similarly, estimator B expands to include bus 1 and bus 5. Instrumentation data, such as 1-5 and 1-5, are also exchanged from A to B.

Therefore, the textured estimator consists of two independent estimators A and B with the overlapping areas including buses 1, 2, and 9. However, estimated data exchange needs extra updating as described below.

# Estimated Data Exchange:

After local estimator A and B have been executed simultaneously and asynchronously, selected estimation result in A, such as 9-14, 9-14 and 9, are exchanged from A to B. In view of these estimated data, B modifies its own estimation result accordingly and re-runs the bad data analysis.

Similarly, selected estimation result in B, such as 1-5, 5-1 and 1, are exchanged from B to A. Taking these estimated data into account, A also modifies its own estimation result accordingly and re-runs the bad data analysis.

#### IV. ESTIMATED DATE EXCHANGE

#### 4.1 Sparse Technique for Matrix Modification

Sparse technique for matrix modification is widely used in power system computation, and the main idea is that instead of re-computing a new sparse matrix, a modification on the old one is processed to reduce its computation complexity. One major technique about the inverse matrix of sparse matrix (A+MaNT) is well known as:

$$(A + MaN^{T})^{-1} = A^{-1} - A^{-1}M(a^{-1} + N^{T}A^{-1}M)^{-1}N^{T}A^{-1}(1)$$

where A is a  $n \times n$  high-dimension sparse square matrix whose inverse matrix  $A^{-1}$  is already computed in advance, and

a is a  $m \times m$  square matrix and m is much less than n.

The computation complexity of re-computing  $(A + MaN^T)^{-1}$  is much higher than that of right side of (1).

# 4.2 Application of the Sparse Technique

In Step 4 of the flowchart, after the estimated data exchange, the succeeding modification on the estimation result of local estimators can be time-consuming if local estimation is executed again from the very beginning. When a sequential SE algorithm, such as orthogonal method based on row-wise Givens rotations [10], is used in local estimator, the speed of such a modification process is fast even without other special techniques because of the nature of the sequential SE algorithm. However, if the conventional Gauss Newton method is utilized in local estimator, it is time-consuming to execute SE again. Therefore, a sparse matrix modification technique is developed to modify the estimation result of local estimators and to avoid re-computing from the very beginning when some estimated data are newly added from other neighboring estimators. Such a technique can significantly accelerate the process in Step 4. Details are discussed below.

As described in Part III, section 2, the SE problem is based on the model [11]:

$$z = h(x) + e \tag{2}$$

where

z represents measurements,

e is the measurement noise vector,

x is the state vector composed of the phase angles and the magnitudes of the voltages on network buses, and

 $h(\bullet)$  stands for the nonlinear measurement functions.

Traditionally a nonlinear iterative algorithm is widely used to solve the SE problem. At each iteration i, the following equations is solved:

$$\Delta x_i = (H^T R^{-1} H)^{-1} H^T R^{-1} \Delta z_i = G^{-1} H^T R^{-1} \Delta z_i$$
 (3)

where

R is the measurement covariance matrix

*H* is the Jacobian matrix  $\partial h/\partial x$ ,

$$\Delta x_i = x_{i+1} - x_i ,$$

$$\Delta z_i = z - h(x_i),$$

 $G = H^{T} R^{-1} H$  is the gain matrix.

The most time-consuming computation in solving (3) is the determination of G and  $G^{-1}$ .

Suppose SE result based on current measurements is already obtained, and then some new data are introduced while the observable island maintains same, that is, the dimension of state variables is fixed.

Then the following equations hold:

$$\begin{bmatrix} z \\ z_{new} \end{bmatrix} = \begin{bmatrix} h(x) \\ h_{new}(x) \end{bmatrix} + \begin{bmatrix} e \\ e_{new} \end{bmatrix} \implies \Delta x_i = \left( \begin{bmatrix} H^T & H_{new}^T \end{bmatrix} \begin{bmatrix} R^{-1} & 0 \\ 0 & R_{new}^{-1} \end{bmatrix} \begin{bmatrix} H \\ H_{new} \end{bmatrix} \right)^{-1} \bullet$$

$$\begin{bmatrix} H^{T} & H_{new}^{T} \end{bmatrix} \begin{bmatrix} R^{-1} & 0 \\ 0 & R_{new}^{-1} \end{bmatrix} \begin{bmatrix} \Delta z \\ \Delta z_{new} \end{bmatrix} = (G + H_{new}^{T} R_{new}^{-1} H_{new})^{-1} (H^{T} R^{-1} \Delta z + H_{new}^{T} R_{new}^{-1} \Delta z_{new})$$
(4)

where the subscript 'new' stands for the newly introduced exchanged estimated data, whose dimension is very low.

Since the new measurements in Step 4 are estimated data with high accuracy, it is reasonable to fix H as a constant during modification process. Therefore,  $(H^T R^{-1} \Delta z)$  and  $G^{-1}$  in (4) are the same as those in the old SE result (3), and they are known before modification process.

Accordingly, considering the dimension of Rnew is much lower than that of G, sparse matrix technique described in (1) can be utilized here to determine  $\left(G + H_{new}^T R_{new}^{-1} H_{new}\right)^{-1}$  in (4). Consequently, the modification is no longer time-consuming.

# V. DETERMINATION OF STATE OVER WHOLE GRID

After the first four steps of the flowchart have been executed, the state over whole grid is determined as follows.

<u>Step 5.1</u>: Determine the angle difference of reference buses between any two local estimators. A reasonable scheme is based on the estimation accuracy of different local estimators, and the scheme is formulated as:

$$\Delta \theta_{AB} = \sum_{i \in I} (\theta_{i,A} - \theta_{i,B}) (c_{i,A}^{-1} + c_{i,B}^{-1}) / \sum_{i \in I} (c_{i,A}^{-1} + c_{i,B}^{-1})$$
 (5)

where  $\Delta\theta_{AB}$  is the angle difference of reference buses between local estimator A and B,

I is the set of all the overlapping buses of estimator A and B,

 $\theta_{i,A}$  is the estimated angle on bus i in estimator A, and

 $c_{{\scriptscriptstyle i},{\scriptscriptstyle A}}$  is the i-th diagonal element of covariance matrix  ${\cal C}={\cal G}^{-1}$  .

Matrix C stands for the variances of estimation errors on bus i in estimator A. Therefore, the magnitude of  $c_{i,A}$  is proportional to the estimation error on bus i in estimator A.

<u>Step 5.2</u>: Select a reference bus of one estimator (e.g. A) as the global reference bus for the whole grid.

<u>Step 5.3</u>: Determine the angle difference between this global reference bus and the reference bus in every local estimator. For local estimators (e.g. B) that connect directly with A, (5) can give the angle difference directly. However, for local estimators (e.g. C) that only connect the neighboring estimators of A (e.g. B) while estimator C itself does not connect with A directly, then the following equation is utilized:

$$\Delta \theta_{AC} = \Delta \theta_{AR} + \Delta \theta_{BC}$$
.

<u>Step 5.4</u>: The estimated angle of each local estimator will be subtracted with the angle difference between the global reference bus and the local difference bus.

<u>Step 5.5</u>: For non-overlapping buses, the state variables are finally determined, which is just the current estimation result in local estimators.

**Step 5.6:** For overlapping bus i belonging to multiple local estimators  $K_j$ , j = 1, 2, ..., m, the state variables  $x_i$  are finally determined as:

$$x_{i} = \sum_{j=1}^{m} (x_{i,K_{j}} c_{i,K_{j}}^{-1}) / \sum_{i=1}^{m} c_{i,K_{j}}^{-1}$$

where  $x_{i,K_i}$  is the state variable of bus i in estimator  $K_j$ .

# VI. NUMERICAL RESULTS

IEEE 14-bus system mentioned before is used to verify that:

- 1. The accuracy and discrepancy performance is satisfied compared to OSE, and higher than the existing DSE algorithm; and
- 2.The bad data detection ability improves greatly than existing DSE algorithm where bad data analysis is executed only in individual local estimators.

# 6.1 Case 1: Accuracy and Discrepancy

Suppose there is a deviation of 0.01 p.u. on power flow measurement 5-2, which is still in the range of tolerance, and no bad data is detected. Table 1 shows concurrent textured DSE algorithm is more accurate than existing DSE algorithm without data exchange.

Accordingly, the discrepancy decreases from 0.007 in existing DSE without data exchange to 0.004 in textured DSE.

Table 1 Estimation Result Derivation

Algorithm	OSE	Existing DSE without data exchange	Textured DSE
Deviation on $\theta_2$	0.003	0.007	0.004

#### 6.2 Case 2: Effect of textured instrumentation data exchange (1)

<u>Bad Data in RTO A</u>: Suppose that 11-10 is bad instrumentation data (where the sign is reversed). Measurements with largest normalized residues will be selected as bad data according to WLS algorithm for SE.

Without Instrumentation Data Exchange (Non-Textured):

For estimator A in Fig. 3, 11-10 can only be detected as bad data, but cannot be identified based on Table 2.

With Instrumentation Data Exchange (Textured):

For estimator A in Fig. 4, 11-10 is identified successfully according to Table 2.

Table 2 Normalized Residues For Local Estimator A

Order	Estimator A in Fig. 3		Estimator A in Fig. 4		
	Meas.	Max.Residue	Meas.	Residue	
1	10	53.38660	11-10	52.40	
	11-10	53.38660	10	46.42	

#### 6.3 Case 3: Effect of textured instrumentation data exchange (2)

Bad Data in RTO B: Suppose that both 2-3 and 2-4 are bad data (all increase by 0.1 p.u.).

Without Instrumentation Data Exchange (Non-Textured):

For estimator B in Fig. 3, 2 and 4 are selected incorrectly as bad data based on Table 3.

With Instrumentation Data Exchange (Textured):

For estimator B in Fig. 4, 2-4 and 2-3 are identified successfully one by one based on Table 3.

Table 3 Normalized Residues For Local Estimator B

Order -	Estimator B in Fig. 3		Estimator B in Fig. 4		
	Meas.	Max. Residue	Meas.	Max. Residue	
1	2	106.8	2-4	94.9	
2	4	44.8	2-3	83.4	

#### 6.4 Case 4: Effect of estimated data exchange

Bad Data In RTO A: Suppose that both 1-5 and 5-1 are bad data (all increased by 0.1 p.u.).

Without Estimated Data Exchange:

Even for estimator A with instrumentation data exchange as shown in Fig. 4, 1 and 5 are still selected incorrectly as bad data according to Table 4.

With Estimated Data Exchange:

Step 1) Estimator A in Fig. 4 with instrumentation data exchange is executed. By now 1 and 5 is still identified incorrectly as bad data by A according to Table 4.

Step 2) Simultaneously, estimator B is executed with instrumentation data exchange as shown in Fig. 4. Then, 1-5 and 5-1 are both identified as bad data successfully one by one based on Table 4. Therefore, estimation results on 1-5 and 5-1 are corrected in estimator B.

Step 3) These corrected values on 1-5 and 5-1 are exchanged from B to A, which follows the estimated data exchange scheme mentioned before. These values are treated in estimator A as pseudo-measurements with particular high accuracy and reliability.

Step 4) Taking the new pseudo-measurements into account, estimator A modifies its own estimation result and re-runs bad data analysis. This time, 1-5 and 5-1 are both successfully identified as bad data in estimator A based on Table 4.

Table 4 Normalized Residues For Local Estimator A and B

Order	Estimator <i>A</i> in Fig. 4		Estimator <i>B</i> in Fig. 4		Estimator <i>A</i> in Fig. 4 with estimated data exchange	
	Meas.	Max. Residue	Meas	Max. Residue	Meas.	Max. Residue
1	1	68.95	5-1	87	5-1	84
2	5	59.4	1-5	84	1-5	94

#### VII. CONCLUSIONS

As noted, there is a recent trend for ISOs/RTOs is to grow toward a Mega-RTO grid. Certainly, the determination of state over the whole system becomes very challenging due to its size. Instead of starting a totally new estimator over the whole grid, a distributed concurrent textured algorithm is proposed to determine the state of whole grid, where the currently existing state estimators distributed in different companies/ISOs/RTOs are fully utilized. The new algorithm is based on extra communication for some instrumentation or estimated data exchange. In addition, such an algorithm is non-recursive, asynchronous, and avoids a central-controlling node. Sparse matrix techniques are also utilized when updating local estimation through estimated data exchanges. Therefore, the new algorithm is fast and practical. Furthermore, based on the developed textured decomposition method, numerical tests verify that the performance of the new textured DSE algorithm greatly improves as compared to existing DSE algorithms, with respect to bad data analysis, estimation accuracy and elimination of discrepancy on boundary buses.

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# **PROJECT CONCLUSIONS**

This project has focused on issues related to state estimation in a new power market operating environment. The first issue is the improvements needed in the measurement design in order to ensure reliable state estimation even under contingency conditions. This is addressed by developing a meter placement method which determines the least cost metering upgrade while accounting for contingencies. Another issue is the incorporation of FACTS devices into the state estimation formulation. This is accomplished by modifying the estimation problem formulation and by including the operation and parameter limits of the FACTS devices. The issue of distributed multi-utility operation is addressed by developing a distributed textured decomposition state estimator and also by devising strategies for efficient measurement exchange between utilities.

The results of the project are implemented with prototype software tested on typical power system configurations.